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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) A system that can measure the attitude of a spinning rocket when coupled with a laser radar tracker was investigated. The attitude sensing system consists of at least two ground based laser transmitter/detector stations which illuminate the rocket with continuous wave lasers as it moves downrange. Pulses that are reflected from two roof type prisms onboard the spinning vehicle back to the two transmitting stations along with position data obtained from the tracking laser radar form the basis for determining the missile's pitch and yaw. A static bench scale demonstration, a dynamic computer simulation and sensitivity analysis of		

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ABSTRACT (cont'd):

→ this concept all continue to support this system as a viable alternative to the current photographic technique for determining missile attitude. ↗

UWME-DR-6051101

**A LASER SYSTEM FOR DETERMINATION OF ROCKET ATTITUDE  
USING TWO GROUND STATIONS**

**Final Report**

by

**John E. Nydahl and Kynric M. Pell**

**December 1976**

**United States Army Research Office  
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**Department of Mechanical Engineering  
University of Wyoming  
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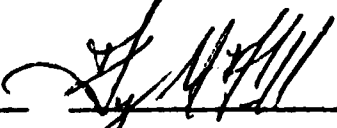
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The concept investigated was developed by personnel at the University of Wyoming and the Aeroballistics Directorate of the United States Army Missile Command Research and Engineering Laboratories. Mr. Robert G. Conard's continuing interest and encouragement has provided a basis for the investigations, which we gratefully acknowledge.

Studies of the use of laser systems for attitude determination of flight vehicles have served as thesis topics for three Master's Degree candidates (Mr. Mark Russell, Mr. Kuen-Der Lain and Mr. Noriyuki Inagaki) over the past three years. We wish to acknowledge their efforts in the investigations described.

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## INTRODUCTION

Measurement of vehicle dynamics during flight on test ranges has been approached using both ground-based and onboard instrumentation. Onboard platforms and accelerometers require telemetry systems or recorders resulting in relatively expensive instrumentation which must be considered expendable in most tests. Onboard solar aspect sensors have been developed for spinning missiles which can be used to infer yawing, pitching and rolling motion of flight vehicles. The most successful of these is the Yawsonde developed at the Ballistic Research Laboratories.<sup>(1,2)</sup> Many flight systems are tested using only ground-based instrumentation employing primarily photographic techniques. Data reduction in these cases is essentially all manual with attendant high cost and relatively long data reduction time.

During the past four years, two novel concepts for measurement of position and attitude have been investigated by the University of Wyoming in cooperation with the U.S. Army Missile Command. The first system investigated incorporated three ground-based laser transmitter/detector stations and expendable retroreflecting elements located on the vehicles. This concept was investigated in considerable detail and the results of the studies are presented in reference 3. Research in the past year has been directed at a simplified system which requires only two ground based stations. When compared to current ground-based photographic techniques for determining both position and attitude,



this system offers several advantages including: lower recurring costs; improved accuracy; automated data reduction; and applicability in low ambient light situations and in situations where the trajectory of the vehicle is not well established prior to flight.

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### SYSTEM CONCEPT

The system includes two ground-based transmitter/detector tracking stations, each incorporating one pulsed and one continuous wave (CW) laser of different frequencies. On board the vehicle, two different types of retroreflecting arrays are required.

One type of array is composed of either conventional corner cubes, reflective tapes and or paints which have the property of retroreflecting a portion of the collimated incident beam back parallel to itself regardless of the orientation of the reflective surface. This array forms a retroreflecting band located on the perimeter of the vehicle body at one axial position. Illumination of and reflection by this retroreflecting band will then form the basis for a conventional laser radar tracking system.

A series of roof type prisms as shown in Figure 1 form a second array which is also mounted on the vehicle's surface. This particular reflector array will be designated here the single plane corner reflector. A plane which passes through the center of all the reflecting surfaces of the roof type array and is also normal to all these surfaces will be called the retroreflection plane. Collimated light incident on the single plane corner reflector and contained in its retroreflection plane ( $\theta=90^\circ$ ) is reflected back to the source. Two of these single plane corner reflectors are mounted on the surface of the vehicle in such a manner that their retroreflection planes are skewed relative to each

other and the roll axis of the vehicle. The mathematical analysis to follow will consider the special case where the retroreflection plane of one of the arrays contains the roll axis. An illustration of an instrumented vehicle is provided in Figure 2.

As the vehicle flies downrange, it is tracked with the laser radar for determining the vehicle position as a function of time while also positioning the CW laser to provide continuous CW illumination of the vehicle. During each revolution of the spinning vehicle, two CW laser pulses are returned to each of the two tracking stations. The time interval between the pulses returned to two separate tracking stations and between the two pulses returned to each station provide sufficient data for determination of the vehicle attitude. A mathematical description of this system is presented in the next section.

# MATHEMATICAL DESCRIPTION OF A SYSTEM

In order to describe the system mathematically, two right-hand orthogonal coordinate systems are utilized: an earth-fixed cartesian system and a vehicle based cartesian system. The earth-fixed system is defined with the origin located at the launch site; positive Z-axis pointing in the vertical upward direction from the center of earth; positive Y-axis in the downrange direction; and positive X-axis in the crossrange direction. The vehicle based system is defined with the origin located at the vehicle center of gravity;  $\omega$ -axis coinciding with the vehicle roll axis with the positive direction pointing toward the nose;  $\eta$ -axis orientated perpendicular to  $\omega$  and parallel to the X-Y plane of the earth-fixed system;  $\xi$ -axis orientated perpendicular to  $\eta$  and  $\omega$  with its positive direction such that  $\eta, \omega, \xi$  form a right hand orthogonal system.

The components of the position vectors of the  $i$ th ground station and the vehicle in the earth-fixed system are  $X_i, Y_i, Z_i$  and  $X_m, Y_m, Z_m$  respectively. Using the well-known transformation between the

$$\begin{pmatrix} \eta_i \\ \omega_i \\ \xi_i \end{pmatrix} = \begin{pmatrix} \cos(\delta_2) & \sin(\delta_2) & 0 \\ \sin(\delta_1) & -\sin(\delta_2)\cos(\delta_1) & \cos(\delta_2)\cos(\delta_1) \\ \cos(\delta_1) & \sin(\delta_1)\sin(\delta_2) & -\sin(\delta_1)\cos(\delta_2) \end{pmatrix} \begin{pmatrix} X_i - X_m \\ Y_i - Y_m \\ Z_i - Z_m \end{pmatrix}$$

earth-fixed and vehicle-fixed systems one obtains the following relationships for the coordinates of the ground stations in the vehicle-fixed coordinates:

$$\begin{aligned}
 \eta_1 &= \cos(\delta_2)(X_1 - X_m) - \sin(\delta_2)(Y_1 - Y_m) \\
 \omega_1 &= \sin(\delta_2)\cos(\delta_1)(X_1 - X_m) + \cos(\delta_2)\cos(\delta_1)(Y_1 - Y_m) \\
 &\quad + \sin(\delta_1)(Z_1 - Z_m) \\
 \xi_1 &= -\sin(\delta_2)\sin(\delta_1)(X_1 - X_m) - \cos(\delta_2)\sin(\delta_1)(Y_1 - Y_m) \\
 &\quad + \cos(\delta_1)(Z_1 - Z_m)
 \end{aligned} \tag{1}$$

where  $\delta_1$  and  $\delta_2$  represent pitch and yaw respectively. Pitch is defined here to be the angle between the X-Y plane and the  $\omega$  axis whereas yaw is defined to be the angle between the YZ plane and the projection of the  $\omega$  axis into the X-Y plane as shown in Figure 3 and 4.

(a) Time Relationship Between Return Pulses

To establish the time relationship between return pulses, we assume that the missile position, attitude and the roll rate do not change during the time interval between the pulse reception at the ground stations. Assume that at time  $t_1$  there is a pulse returned to the first ground station from the skewed corner reflector as shown in Figures 5 through Figure 7. At this moment if the position vectors of ground station 1 and 2 are  $\eta_1, \omega_1, \xi_1$  and  $\eta_2, \omega_2, \xi_2$ , then it can be observed that, with a constant roll rate  $\Omega$  for the flight vehicle, the time interval for reception of a second pulse from the second single

plane array at the same station is

$$\Delta t_{11} = \frac{1}{\Omega} [2\pi - (\alpha - \theta_S)] \quad (2)$$

The time interval between pulses returned from the first array to the two different ground stations is:

$$\Delta t_{21} = \frac{1}{\Omega} (\theta_1 - \theta_2) \quad (3)$$

In terms of  $\eta\omega\xi$  coordinates, Eq. (2) can be written as

$$\Omega \Delta t_{11} = 2\pi - \alpha - \arcsin \left[ \frac{\omega_1 \tan(\gamma)}{(\eta_1^2 + \xi_1^2)^{1/2}} \right] \quad (4)$$

and Eq. (3) may be written as

$$\Omega \Delta t_{21} = \arctan\left(\frac{\xi_1}{\eta_1}\right) - \arctan\left(\frac{\xi_2}{\eta_2}\right) \quad (5)$$

Substituting Eq. (1) into Eqs. (4) and (5), it may be seen that the right sides of Eqs. (4) and (5) are functions of only two unknowns, that is, pitch ( $\delta_1$ ) and yaw ( $\delta_2$ ). The relative positions are assumed to be known from tracking data. Since  $\Delta t_{11}$ ,  $\Delta t_{21}$  and  $\Omega$  can be determined using data from the C.W. laser system, Eqs. (4) and (5) can in principle be solved for the pitch and yaw, using, for example, the Newton-Raphson technique.

#### (b) Mathematical Approach for Simulation

The mathematical description presented in the previous section assumed that the vehicle was fixed in space, and that  $\Omega$ ,  $\delta_1$  and  $\delta_2$  did not vary during the time intervals  $\Delta t_{11}$  and  $\Delta t_{21}$ . In the situation

that arises during an actual flight test not only is the vehicle position changing but also  $\Omega$ ,  $\delta_1$  and  $\delta_2$  may vary. One approach to data reduction of flight test data would be to analyze the data as though the vehicle did meet the assumptions described in the previous section recognizing that some error could be introduced due to the vehicle dynamics. In order to gain some insight into the errors in the pitch and yaw angles determined using the static analysis a computer simulation a rocket trajectory was developed. The simulation provides the missile position and attitude as a function of time as well as the time at which pulses would be received from the two retroreflectors at the two ground stations. For this study a six degree of freedom trajectory simulation originally developed by Harris<sup>(4)</sup>, and later modified by Russell<sup>(3)</sup> was again modified. The program developed by Russell was used to study the three ground station laser concept mentioned previously. Only those additional modifications required to simulate the two ground station - two single plane retroreflector concept are described here.

In the original program, two right-hand orthogonal coordinate systems are defined: an earth-fixed coordinate system and a body-fixed coordinate system. The coordinate systems used in this thesis also include an earth-fixed and a body-fixed system, however, they are defined differently than the original systems. The relationships between the coordinates originally defined and those used in this analysis

may be seen in Figure 8. The body-fixed coordinates are obtained by rotating the earth-fixed system through three angles,  $\lambda$ ,  $\mu$ , and  $\nu$  as shown in Figure 9. Other information which is needed in the mathematical approach of the simulation includes the direction cosines. These are defined in Figure 10. Then we have, from Figure 11 through Figure 13.

$$\begin{aligned}\delta_1 &= -\arcsin(l_3) \\ \delta_2 &= \arctan\left(\frac{l_2}{l_1}\right)\end{aligned}\tag{6}$$

To determine the values of pitch ( $\delta_1$ ) and yaw ( $\delta_2$ ) at the moment when stations have return pulses, it is necessary to define an angle which is called the corner reflector angle (CRA). Suppose at time  $t \leq 0$  the skewed and straight corner reflectors are arranged on the rocket in the  $\eta\omega\xi$  coordinate system as shown in Figure 14. Imagine that the rocket is rotating in the clockwise direction. Then if at time  $t = t'$ , ground station 1 has a return pulse from the straight corner reflector, the rocket must be orientated in the  $\eta\omega\xi$  coordinates as shown in Figure 15. Considering this situation and referring to Figure 16 the corner reflector angle (CRA) can be defined as

$$\text{CRA} = \arctan\left(\frac{m_3}{n_3}\right)\tag{7}$$

However, at this moment, the orientation for the position vector of the station 1 in  $\eta\omega\xi$  coordinate system is



$$\theta_1 = \arctan\left(\frac{\xi_1}{\eta_1}\right) \quad (8)$$

This implies that the criteria to ensure pulses are returned from the straight corner reflector to station 1 is

$$\arctan\left(\frac{m_3}{n_3}\right) = \arctan\left(\frac{\xi_1}{\eta_1}\right) \quad (9)$$

This concept can also be extended to ground station 2. Therefore, we can put the criteria to have pulses returned from the straight corner reflector in the general form:

$$\arctan\left(\frac{m_3}{n_3}\right) = \arctan\left(\frac{\xi_1}{\eta_1}\right) \quad (10)$$

To get a condition that station 1 has the signal returned from the skewed corner reflector, assume that at time = t, the rocket is orientated in the  $\eta\xi\omega$  coordinate system as shown in Figure 15 and that station 1 has a pulse reception. Then, from the geometry, we have

$$\alpha - \theta_s = \text{CRA} + \theta_1 \quad (11)$$

Where  $\theta_1$  can be expressed as

$$\theta_1 = \arcsin\left[\frac{\omega_1 \tan \gamma}{(\eta_1^2 + \xi_1^2)^{1/2}}\right] \quad (12)$$

From Eq. (7) through Eq. (12) we obtain

$$\alpha = \arcsin\left[\frac{\omega_1 \tan \gamma}{(\eta_1^2 + \xi_1^2)^{1/2}}\right]$$

$$= \arctan\left(\frac{\eta_3}{\eta_1}\right) + \arctan\left(\frac{\xi_1}{\eta_1}\right) \quad (13)$$

Eq. (13) is the criteria for pulse return at the station 1 from the skewed corner reflector. Similarly, for ith ground station to have pulses returned, the mathematical expression is the same as Eq. (13) except we replace 1 by i.

### (c) Sensitivity Analysis

In the previous sections, when the equations for the returned pulses were set up to determine pitch and yaw, it was assumed that the missile position, attitude and roll rate did not change during the time intervals which were related to the actual reception of pulses at the two ground stations for the skewed and straight corner reflectors. As has been mentioned, the time intervals between returned pulses are influenced by the dynamic change of the missile position, attitude and roll rate. To determine the magnitude of the error which may be introduced by approximating the actual dynamic situation with a steady state model, we will define the following time intervals:  $\Delta t_{ii}^o$  is the observed time interval between the passing of the skewed and straight retroreflection planes through the ith ground station.  $\Delta t_{ii}^n$  is the corresponding time interval predicted by the steady state model where the actual kinematic state occurring at the first received pulse is taken as the steady kinematic state of the missile.  $\Delta t_{ij}^o$  is the observed time interval between the

passing of the straight retroreflection plane through the  $i$ th and  $j$ th ground stations.  $\Delta t_{ij}^n$  is the corresponding time interval predicted by the steady state model where the mean position, mean pitch and yaw, and mean roll rate occurring between the two pulse times are used as the steady kinematic state of the missile,

If the differences between the observed time intervals ( $\Delta t_{ij}^o$  and  $\Delta t_{ii}^o$ ) and the corresponding time intervals predicted from the steady state model ( $\Delta t_{ij}^n$  and  $\Delta t_{ii}^n$ ) are small, a linear variation between the two sets of time intervals in terms of kinematic differences may be appropriate. If this be the case, then the maximum error generated by the steady state model is approximately

$$\Delta t_{ii}^o - \Delta t_{ii}^n \leq \left[ \sum_K \left( \frac{\partial \Delta t_{ii}^n}{\partial \phi_K} \right)_{t_1}^2 (\phi_{K,t_1} - \phi_{K,t_2})^2 \right]^{1/2} \quad (14)$$

$$\Delta t_{ij}^o - \Delta t_{ij}^n \leq \left[ \sum_K \left( \frac{\partial \Delta t_{ij}^n}{\partial \phi_K} \right)_{t_n}^2 (\phi_{K,t_2} - \phi_{K,n})^2 \right]^{1/2} \quad (15)$$

where  $t_1$  and  $t_2$  designate the time when the  $i$ th ground station has the actual pulse reception,  $\phi_{K,t_1}$  represents the  $k$ th kinematic parameter evaluated at time  $t_1$ , and  $\phi_{K,n}$  represents the mean value of the kinematic parameter related to  $\Delta t_{ij}^n$ . The terms  $\left( \frac{\partial \Delta t_{ii}^n}{\partial \phi_K} \right)_{t_1}$  and  $\left( \frac{\partial \Delta t_{ij}^n}{\partial \phi_K} \right)_{t_n}$  are the sensitivities of the time intervals  $\Delta t_{ii}^n$  and  $\Delta t_{ij}^n$ . The parameter  $\phi_K$  includes variables  $\delta_1$ ,  $\delta_2$ ,  $\Omega_K$ ,  $X_m$ ,  $Y_m$  and  $Z_m$ . The various sensitivities are classified into two categories for the skewed reflector and the straight reflector.

#### (1) The Skewed System

The various sensitivities for this system are pitch, yaw, altitude, range, crossrange, and roll rate. Mathematically they correspond to

$$\frac{\partial \Delta t_{ii}}{\partial \delta_1}, \frac{\partial \Delta t_{ii}}{\partial \delta_2}, \frac{\partial \Delta t_{ii}}{\partial Z_m}, \frac{\partial \Delta t_{ii}}{\partial Y_m}, \frac{\partial \Delta t_{ii}}{\partial X_m} \text{ and } \frac{\partial \Delta t_{ii}}{\partial \Omega} \text{ respectively. Thus, if}$$

we use Eq. (4) and the parameter  $P_K$  to denote the variables  $\delta_1$ ,  $\delta_2$ ,

$X_m$ ,  $Y_m$ , and  $Z_m$ . We obtain

$$\frac{\partial \Delta t_{11}}{\partial P_K} = \frac{\tan \gamma \left[ \frac{\omega_1}{\eta_1^2 + \xi_1^2} \left( \eta_1 \frac{\partial \eta_1}{\partial P_K} + \xi_1 \frac{\partial \xi_1}{\partial P_K} \right) - \frac{\partial \omega_1}{\partial P_K} \right]}{\Omega (\eta_1^2 + \xi_1^2 - \omega_1^2 \tan^2 \gamma)^{1/2}} \quad (16)$$

and

$$\frac{\partial \Delta t_{11}}{\partial \Omega} = \frac{1}{\Omega^2} \{ \alpha + \arcsin \left[ \frac{\omega_1 \tan \gamma}{(\eta_1^2 + \xi_1^2)^{1/2}} \right] - 2\pi \} \quad (17)$$

## (2) The Straight System

The various sensitivities in this system have the same notation as in the skewed system except we replace  $\Delta t_{11}$  by  $\Delta t_{1j}$ . If  $P_K$  indicates the variables  $\delta_1$ ,  $\delta_2$ ,  $X_m$ ,  $Y_m$ ,  $Z_m$ , then, from Eq. (5), the sensitivities are as follows:

$$\frac{\partial \Delta t_{1j}}{\partial P_K} = \frac{1}{\Omega} \left\{ \left[ \frac{\eta_j \frac{\partial \xi_j}{\partial P_K} - \xi_j \frac{\partial \eta_j}{\partial P_K}}{\eta_j^2 + \xi_j^2} \right] - \left[ \frac{\eta_1 \frac{\partial \xi_1}{\partial P_K} - \xi_1 \frac{\partial \eta_1}{\partial P_K}}{\eta_1^2 + \xi_1^2} \right] \right\} \quad (18)$$

and

$$\frac{\partial \Delta t_{1j}}{\partial \Omega} = \frac{1}{\Omega^2} \left[ \arctan \left( \frac{\xi_j}{\eta_j} \right) - \arctan \left( \frac{\xi_1}{\eta_1} \right) \right] \quad (19)$$

The expressions for the sensitivities can be rewritten using equations

(1) and the expressions presented below:

$$\frac{\partial \eta_1}{\partial \delta_1} = 0 \quad (20)$$

$$\frac{\partial \eta_1}{\partial \delta_2} = -(X_1 - X_m) \sin(\delta_2) - (Y_1 - Y_m) \cos(\delta_2) \quad (21)$$

$$\begin{aligned} \frac{\partial \xi_1}{\partial \delta_1} = & -(X_1 - X_m) \sin(\delta_2) \cos(\delta_1) - (Y_1 - Y_m) \cos(\delta_2) \cos(\delta_1) \\ & - (Z_1 - Z_m) \sin(\delta_1) \end{aligned} \quad (22)$$

$$\frac{\partial \xi_1}{\partial \delta_2} = -(X_1 - X_m) \cos(\delta_2) \sin(\delta_1) + (Y_1 - Y_m) \sin(\delta_2) \sin(\delta_1) \quad (23)$$

$$\begin{aligned} \frac{\partial \omega_1}{\partial \delta_1} = & -(X_1 - X_m) \sin(\delta_2) \sin(\delta_1) - (Y_1 - Y_m) \cos(\delta_2) \sin(\delta_1) \\ & + (Z_1 - Z_m) \cos(\delta_2) \end{aligned} \quad (24)$$

$$\frac{\partial \omega_1}{\partial \delta_2} = (X_1 - X_m) \cos(\delta_2) \cos(\delta_1) - (Y_1 - Y_m) \sin(\delta_2) \cos(\delta_1) \quad (25)$$

$$\frac{\partial \eta_1}{\partial X_m} = -\cos(\delta_2) \quad (26)$$

$$\frac{\partial \eta_1}{\partial Y_m} = \sin(\delta_2) \quad (27)$$

$$\frac{\partial \eta_1}{\partial Z_m} = 0 \quad (28)$$

$$\frac{\partial \xi_1}{\partial X_m} = \sin(\delta_2) \sin(\delta_1) \quad (29)$$

$$\frac{\partial \xi_1}{\partial Y_m} = \cos(\delta_2) \sin(\delta_1) \quad (30)$$

$$\frac{\partial \xi_1}{\partial Z_m} = -\cos(\delta_1) \quad (31)$$

$$\frac{\partial \omega_1}{\partial X_m} = -\sin(\delta_2)\cos(\delta_1) \quad (32)$$

$$\frac{\partial \omega_1}{\partial Y_m} = -\cos(\delta_2)\cos(\delta_1) \quad (33)$$

$$\frac{\partial \omega_1}{\partial Z_m} = -\sin(\delta_1) \quad (34)$$

#### (d) Error Analysis

One approach to the data reduction would be to analyze the data as though the vehicle were fixed in space, with a fixed attitude (pitch and yaw) and a constant roll rate. The effect of vehicle dynamics would be to introduce an error into the values of pitch and yaw calculated from the measured time intervals. In order to obtain an estimate of the magnitude of the error that could be introduced through this mechanism and also provide some insight with respect to which parameters play a dominant role in contributing to this error, the six degree of freedom simulation was exercised. The two ground stations were assumed to be located at 3000, 0, 0 and 3000, 2000, 0. Parameters for the geometry of the skewed retroreflectors which had to be preassigned included  $\alpha$ , the circumferential angle, and  $\gamma$ , the inclination. Values of  $60^\circ$  and  $15^\circ$  were chosen for the respective quantities.

The output from the simulation run included:

a) For pulses retroreflected from the straight reflector

1. The time of pulse reception at ground station

- number 1. (TIME1)
- 2. The time of pulse reception at ground station  
number 2. (TIME2)
- 3. The time difference between pulse reception at  
the two stations. (DTIME12)
- 4. The time difference between DTIME12 and the nominal time interval  $\Delta t_{ij}^n$ . (DTMF12)
- 5. The missile position midway between the positions  
at the time of pulse receptions. (XM, YM, ZM)
- 6. The average values of pitch, yaw and roll rate  
during the time interval DTIME12. (PITCH, YAW, ROLL).
- 7. The difference in the average and the extreme  
values for missile position during the interval  
DTIME12. (DXM, DYM, DZM)
- 8. The difference between the average and the extreme  
values of pitch, yaw and roll rate during the interval DTIME12. (DPITCH, DYAW, DROLL)
- 9. The sensitivity of the time interval to: Pitch,  
yaw, crossrange, altitude and a time midway between  
TIME1 and TIME2. (PITCH, YAWS, CROS, RANS, ALTS,  
ROLLS)
- b) For pulse retroreflected from the skewed reflector
  - 1. The ground station receiving the return pulse. (GSNO)
  - 2. The time at which a pulse is received at a particular  
station. (TIMES)

3. Geometry related parameters described in the previous list.

These results are presented in tabular form in the following section.



## RESULTS

The six degree of freedom trajectory simulation was given the mass and aerodynamic properties of a tactical rocket (ARROW) recently tested at the U.S. army missile command. This vehicle was selected as representative of the type of vehicle for which a laser system might be used in a flight test program. Information which was derived from the simulation included:

1. Pulse reception time at the two ground stations from the two retroreflectors.
2. Vehicle attitude, roll rate and position at the time of each pulse reception.

This information was then used in a Newton-Raphson solution of Eqs. (4) and (5) to provide calculated values of pitch ( $\delta_1$ ) and yaw ( $\delta_2$ ). It should be noted that average values of the geometric parameters were used in this solution which introduces the errors due to vehicle dynamics discussed previously. The pitch and yaw values obtained in this manner are presented in Table 1 where the values obtained from the simulation as well as the difference between the simulation and calculated results are also tabulated for comparison.

The maximum difference between the simulation result and the calculated pitch is  $0.81^\circ$ , with an average difference of  $0.15^\circ$ , and a most probable difference of  $0.03^\circ$ . It is interesting to note that this

TABLE 1. COMPARISON OF PITCH AND YAW FROM CALCULATION AND SIMULATION

TIMES	19830E-01	13752E 00	25177E 00	35914E 00	45632E 00	54073E 00
XM	-1239E-18	-14002E-02	-12653E-01	-34952E-C1	-73794E-01	-13647E 00
YM	10138E 00	10430E 02	41971E 02	92333E 02	5636E 03	22783E 03
ZM	53132E-02	49519E 00	17328E 01	35799E 01	57697E 01	78491E 01
PITCH(S)	30000E 01	30024E 01	29491E 01	25245E 01	17272E 01	12554E 01
PITCH(C)	30100E 01	29741E 01	26255E 01	18582E C1	12836E C1	13908E 01
YAW(S)	-40712E-16	84885E-04	-17904E-02	-25100E-01	-77917E-01	-77320E-01
YAW(C)	26030E-01	20916E-01	98488E-02	-10473E 00	-19879E 00	-74494E-01
DP11	99915E-02	28244E-01	32358E 00	66629E C0	44368E 00	13242E 00
DYA	26030E-01	20831E-01	11639E-01	79682E-C1	12087E C0	25026E-01



TABLE 1. COMPARISON OF PITCH AND YAW FROM CALCULATION AND SIMULATION  
(CONTINUED)

(CONTINUED)						
TIMES	87447E 00	90278E 00	92865E 00	95248E 00	97456E 00	99515E 00
XXM	-66575E 00	-73574E 00	-80247E 00	-86685E 00	-93004E 00	-99300E 00
YMM	62857E 03	67081E 03	71052E 03	74801E C3	78354E 03	81731E 03
ZYM	16811E 02	17575E 02	18250E 02	18919E 02	19543E 02	20062E 02
PITCH(S)	11771E 01	11382E 01	10220E 01	90344E 00	83748E 00	83543E 00
PITCH(C)	11511E 01	10425E 01	91977E 00	84367E 00	83242E 00	86705E 00
YAW(S)	-50258E-01	-62055E-01	-10214E 00	-14197E 00	-15746E 00	-14434E 00
YAW(C)	-65407E-01	-13623E 00	-19008E 00	-19936E 00	-16709E 00	-11700E 00
DPIT	25985E-01	95672E-01	10222E 00	99778E-01	50674E-02	31616E-01
DAYA	15149E-01	74180E-01	87945E-01	97391E-01	96341E-02	26539E-01

TABLE 1 COMPARISON OF PITCH AND YAW FROM CALCULATION AND SIMULATION  
(CONTINUED)

[illegible]











difference, or pitch error, is distributed along the downrange direction with a maximum at the two extremes and a minimum near midrange. (see Figure 17)

The maximum difference between the simulation result and the calculated yaw is  $1.44^\circ$  whereas the average difference is  $0.18^\circ$ . The most probable error is  $0.04^\circ$ . Referring to Figure 17 it may be seen that the yaw error is also range sensitive. In contrast to the pitch error distribution which shows a degradation in performance at each end of the range shown, the yaw error is large only at the extreme downrange positions. In order to investigate the sources of these errors the sensitivity analysis described in the previous chapter was initiated. The simulation was again used to generate the pulse reception times for the two reflectors and two ground stations. In addition the program was modified to calculate and print out the various sensitivities and perturbation terms. As described in the previous discussion the calculations were done in two groups that is for the straight retroreflector with pulse reception at two different stations and for the skewed retroreflector system with pulse reception from the straight and skewed retroreflectors at the same station. The results are presented in Table 2 and 3 respectively. By multiplying the listed sensitivities by the appropriate perturbation terms the influence of each of the parameters on the time interval  $\Delta t_{11}$  or  $\Delta t_{1j}$  may be obtained. The results of this operation are presented in abbreviated form in Table 4. In the interests of clarity only the order of magnitude of the parameters is indicated. It is immediately apparent that the error introduced by roll dynamics dominates the errors in  $\Delta t_{11}$ . On the other hand roll,

position (range) and pitch dynamics all contribute to the errors in  $\Delta t_{12}$  in a substantial way. Relative magnitudes of the yaw and pitch contribution to the  $\Delta t$  errors may be thought of as yaw/pitch coupling in the  $\Delta t$  equation (Eqs. (4) and (5)). The  $\Delta t_{12}$  equation is weakly coupled to yaw throughout the first 1000 ft of flight and thereafter the magnitude of the pitch and yaw contributions become comparable. On the other hand the  $\Delta t_{11}$  equation is weakly coupled to pitch beyond 1000 feet and at ranges less than 1000 feet the pitch and yaw terms are comparable. A general observation which appears to hold for every parameter tabulated is the fact that the influence on the associated  $\Delta t$  is strongest at the shortest ranges and longest ranges with a minimum in the region of 1000 feet.

TABLE 2 VARIATIONS AND SENSITIVITIES OF STRAIGHT SYSTEM

TIME4	.11908E 00	.23317E 00	.34199E 00	.44116E 00	.52784E 00	.60145E 00
TIME2	.11873E 00	.23379E 00	.34249E 00	.44143E 00	.52803E 00	.60162E 00
TIMEF12	.64932E-03	.61920E-03	.50781E-03	.32030E-03	.18972E-03	.17373E-03
TIMEF12	-.32298E-06	-.41460E-06	-.67683E-06	-.53011E-06	-.10902E-06	-.19451E-06
XA	-.61826E-03	-.10084E-01	-.30442E-01	-.65906E-01	-.12479E 00	-.20233E 00
YM	.72302E 01	.35435E 02	.83011E 02	.14567E 03	.11643E 03	.28675E 03
ZM	.35901E 00	.14847E 01	.32458E 01	.54069E 01	.75625E 01	.94458E 01
PITCH	.30007E 01	.29753E 01	.26277E 01	.18595E 01	.12823E 01	.13703E 01
YAW	.23011E-04	-.71076E-03	-.18863E-01	-.69031E-01	-.10142E 00	-.52524E-01
ROLL	-.30766E 04	-.31985E 04	-.34422E 04	-.38577E 04	-.44972E 04	-.53243E 04
DXM	.10626E-04	.40937E-04	.64405E-04	.79851E-04	.83494E-04	.10485E-03
DYM	-.48436E-01	-.10580E 00	-.13620E 00	-.11720E 00	-.84861E-01	-.87118E-01
DZM	-.21465E-02	-.40365E-02	-.49049E-02	-.38380E-02	-.24105E-02	-.22433E-02
SPITCH	-.18080E-04	.36227E-03	.14460E-02	.14206E-02	.15642E-03	-.37564E-03
DYAW	-.63141E-05	.14076E-04	.85601E-04	.96641E-04	-.51231E-05	-.72416E-04
DROLL	.17637E 00	.42089E 00	.77550E 00	.70487E 00	.89339E 00	.11547E 01
PITCH45	-.21513E-03	-.20771E-03	-.17326E-03	-.17253E-03	-.14803E-03	-.12507E-03
YAW3	-.75030E-05	-.70319E-05	-.56117E-05	-.34790E-05	-.20889E-05	-.18274E-05
CROSS	-.21637E-06	-.20637E-06	-.16735E-06	-.10683E-06	-.63193E-07	-.57722E-07
RANS	-.32495E-05	-.30994E-06	-.25451E-06	-.16067E-06	-.95323E-07	-.87197E-07
ALTS	.75353E-04	.71316E-04	.63171E-04	.63184E-04	.60555E-04	.36348E-04
ROLLS	.21115E-06	.17372E-06	.14772E-06	.83168E-07	.42212E-07	.32667E-07



TABLE 2 VARIATIONS AND SENSITIVITIES OF STRAIGHT SYSTEM  
(CONTINUED)

[illegible]

**TABLE 2 VARIATIONS AND SENSITIVITIES OF STRAIGHT SYSTEM**  
(CONTINUED)

(CONTINUOUS)						
TIME1	.10298E 01	.10471E 01	.10635E 01	.10790E 01	.10939E 01	.11080E 01
TIME2	.10298E 01	.10471E 01	.10635E 01	.10791E 01	.10939E 01	.11080E 01
TIME12	.30035E-04	.29147E-04	.27419E-04	.24850E-04	.22074E-04	.19337E-04
TIME12	-.52950E-06	-.64340E-06	-.63031E-06	-.66173E-06	-.57842E-06	-.60198E-06
TIME4	-.11102E 01	-.11741E 01	-.12377E 01	-.13001E 01	-.13603E 01	-.14176E 01
TIME4	.87566E 03	.90534E 03	.93392E 03	.96140E 03	.98791E 03	.10135E 04
TIME4	.20977E 02	.21426E 02	.21846E 02	.22242E 02	.22618E 02	.22775E 02
PITCH	.91274E 00	.93877E 00	.94979E 00	.98712E 00	.92393E 00	.75804E 00
TIME4	-.85273E-01	-.68416E-01	-.76353E-01	-.10711E 00	-.14968E 00	-.14387E 00
TIME4	.19983E 05	-.20935E 05	-.22073E 05	-.23149E 05	-.24202E 05	-.25222E 05
TIME4	.53919E-04	.55474E-04	.54301E-04	.50342E-04	.44806E-04	.38770E-04
TIME4	-.25630E-01	-.25254E-01	-.24072E-01	-.22102E-01	-.19851E-01	-.17638E-01
TIME4	.39212E-03	.37638E-03	.35071E-03	.31533E-03	-.27890E-03	-.24446E-03
PITCH4	.34012E-04	-.75345E-05	.23647E-04	.46237E-04	.51375E-04	.42539E-04
TIME4	-.23130E-04	-.39030E-05	.17683E-04	.12315E-04	.33179E-04	.22155E-04
TIME4	.93704E 00	.95022E 00	.92938E 00	.87569E 00	.79021E 00	.71241E 00
PITCH5	-.33505E-04	-.31746E-04	-.30182E-04	-.28781E-04	-.27528E-04	-.26416E-04
TIME4	-.27543E-05	-.25789E-05	-.23967E-06	-.22279E-06	-.20844E-06	-.19543E-06
CROSS	-.10175E-07	-.99139E-08	-.93382E-08	-.84912E-08	-.75359E-08	-.66434E-08
TRANS	-.15340E-07	-.14940E-07	-.14371E-07	-.12816E-07	-.11402E-07	-.10080E-07
TIME4	.11072E-08	.87518E-09	.91006E-09	.11559E-08	.14869E-08	.17526E-08
TIME4	.15372E-04	.14175E-08	.12701E-08	.11021E-08	.93598E-09	.79251E-09

TABLE 2 VARIATIONS AND SENSITIVITIES OF STRAIGHT SYSTEM  
(CONTINUED)

(CONTINUOUS)									
TIME-1	.11216E 01	.11347E 01	.11472E 01	.11594E C1	.11712E 01	.11825E 01			
TIME-2	.11216E 01	.11347E 01	.11473E 01	.11594E C1	.11712E 01	.11825E 01			
TIME-12	.17357E-04	.16049E-04	.15663E-04	.15491E-04	.15846E-04	.16297E-04			
TIME-12	-.54599E-06	-.53751E-06	-.57083E-06	-.59872E-06	-.65757E-06	-.69322E-06			
XY	-.14719E 01	-.15236E 01	-.15741E 01	-.16256E C1	-.16804E 01	-.17407E 01			
YY	.10384E 04	.10525E 04	.10659E 04	.10808E 04	.11311E 04	.11529E 04			
ZZ	.23313E 02	.23643E 02	.23972E 02	.24275E 02	.24572E 02	.24857E 02			
PITCH	.70586E 00	.67791E 00	.67766E 00	.70167E C0	.74131E 00	.78409E 00			
YAW	-.21064E 00	-.20079E 00	-.17693E 00	-.14709E C0	-.77516E-01	-.39339E-01			
ROLL	-.26211E 05	-.27172E 05	-.29105E 05	-.39016E 05	-.29904E 05	-.30711E 05			
QCM	.344335E-04	.31827E-04	.31703E-04	.34223E-04	.39346E-04	.45015E-04			
QYM	.15948E-01	-.14890E-01	-.14484E-01	-.14637E-C1	-.15100E-01	-.15642E-01			
QZM	-.21917E-03	-.20524E-03	-.19625E-03	-.19631E-03	-.19911E-03	-.20139E-03			
DPITCH	.27041E-04	.90339E-05	-.84210E-05	-.29464E-04	-.50096E-04	-.30179E-04			
QYAW	.64839E-05	-.10764E-04	-.25712E-04	-.34040E-04	-.32448E-04	-.18494E-04			
QROLL	.63520E 00	.59900E 00	.57671E 00	.58259E C0	.60073E C0	.62223E 00			
PITCHS	-.25421E-04	-.24524E-04	-.23709E-04	-.29644E-04	-.22201E-04	-.21651E-04			
YAWs	-.19593E-05	-.17473E-05	-.17131E-06	-.16389E-06	-.15630E-06	-.14945E-05			
CLOS	-.59507E-08	-.55125E-08	-.53308E-08	-.53526E-08	-.54734E-08	-.55574E-08			
RAVS	-.90381E-08	-.83723E-08	-.80326E-08	-.80929E-C8	-.82812E-08	-.85194E-08			
ALTS	.18746E-08	.17734E-08	.14788E-08	.10691E-03	.65875E-09	.36799E-09			
ROLLS	.58304E-09	.61040E-09	.57047E-09	.55452E-09	.55169E-09	.55215E-09			







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TIME1	.13068F 01	.13149E 01	.13229E 01	.13308E 01	.13385E 01	.13460E 01
TIME2	.13068E 01	.13150E 01	.13230E 01	.13309E 01	.13385E 01	.13461E 01
TIME12	.14397E-04	.23703E-04	.35700E-04	.48713E-04	.57088E-04	.61340E-04
TIME12	-.93207E-05	-.14704E-05	-.25811E-05	-.37137E-05	-.46172E-05	-.48705E-05
XX	-.22643E 01	-.25698E 01	-.31235E 01	-.39193E 01	-.48943E 01	-.58413E 01
YM	.14013E 04	.14195E 04	.14353E 04	.14519E 04	.14681E 04	.14843E 04
ZM	.28243E 02	.28535E 02	.28724E 02	.28970E 02	.29500E 02	.27514E 02
PITCH	.73641E 00	.15744E 01	.24422E 01	.33977E 01	.41674E 01	.43344E 01
YAW	.11599E 01	.13163E 01	.10623E 01	.15486E 00	-.16484E 01	-.45216E 01
ROLL	-.40854E 05	-.41596E 05	-.41336E 05	-.41977E 05	-.43759E 05	-.44537E 05
DOX	.19380E-03	.62110E-03	.14775E-02	.46110E-02	.37139E-02	.32179E-02
DOY	-.14954E-01	-.23774E-01	-.37701E-01	-.51464E-01	-.62862E-01	-.65708E-01
DOZ	-.35424E-02	-.53437E-03	-.47219E-03	.36531E-03	.26512E-02	.63219E-02
DOPTCH	-.46912E-03	-.11153E-02	.20807E-02	-.28930E-02	-.22029E-02	.17379E-02
DOYA	-.26132E-03	-.17562E-04	.11343E-02	.40074E-02	.89795E-02	.14304E-01
DOZLL	.64849E 00	.10753E 01	.16725E 01	.47883E-04	-.78940E-04	.29575E 01
PITCHS	-.16223E-04	-.15713E-04	-.15635E-04	-.15437E-04	-.15313E-04	-.15374E-04
YAWs	-.92978E-07	-.50218E-07	.16295E-07	.12082E-06	.27297E-06	.44093E-06
CRDS	-.51503E-08	-.35307E-08	-.12677E-07	-.17443E-07	-.21307E-07	-.22604E-07
RAVS	-.73036E-08	-.12136E-07	-.13471E-07	-.26067E-07	-.33610E-07	-.37941E-07
ALTS	-.61843E-08	-.68703E-08	-.54203E-08	-.76419E-09	.82209E-08	.22672E-07
ROLLS	.37620E-09	.61491E-09	.90873E-09	.12194E-08	.14559E-08	.14865E-08

TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM

GSNU	1	2	1	2	1	2	1	2
TIMES	.19830E-01	.23877E-01	.13752E 00	.14147E 00	.25177E 00	.25554E 00		
XM	-.11238E-13	-.93310E-17	-.14002E-02	-.16021E-02	-.12653E-01	-.13272E-01		
YM	.10138E 00	.15361E 00	.10430E 02	.11157E 02	.41971E 02	.43394E 02		
ZM	.53132E-02	.80503E-02	.49519E 00	.52596E 00	.17328E 01	.17925E 01		
PITCH	.30000E 01	.30000E 01	.30024E 01	.30027E 01	.19471E 01	.27474E 01		
YAW	-.40712E-15	.74015E-15	.84835E-04	.10535E-03	-.17904E-02	-.20927E-02		
ROLL	-.30270E 04	-.30309E 04	-.33874E 04	-.30877E 04	-.32297E 04	-.32359E 04		
DTMF	-.23675E-05	.67124E-08	-.18610E-05	-.77573E-05	-.10133E-05	-.64153E-04		
CKM	-.60764E-03	-.62987E-03	-.86432E-02	-.35232E-02	-.17724E-01	-.17274E-01		
DYM	.71304E 01	.71750E 01	.24977E 02	.24382E 02	.40904E 02	.37754E 02		
DYM	.35155E 00	.35311E 00	.94551E 00	.96282E 00	.25082E 01	.14542E 01		
DPITCH	.65164E-03	.68784E-03	-.26706E-01	-.27972E-01	-.31990E 00	-.31637E 00		
DYAW	.22380E-04	.23643E-04	-.73157E-03	-.83018E-03	-.16987E-01	-.15456E-01		
ROLL	-.47475E 02	-.45287E 02	-.11059E 03	-.10922E 03	-.1216E 03	-.20704E 03		
PITCHS	-.17127E-17	.45196E-05	-.14910E-08	.44194E-05	-.11940E-07	.40765E-05		
YAWS	-.88340E-04	-.12736E-03	-.86670E-04	-.12644E-03	-.52885E-04	-.11949E-03		
CROS	.57173E-10	-.11402E-05	.57690E-08	-.11121E-05	.22189E-07	-.10442E-05		
RAVS	.16372E-05	.17105E-05	.16552E-05	.16776E-05	.15827E-05	.14011E-05		
ALTS	.88421E-07	.12943E-06	.86917E-07	.12687E-06	.81537E-07	.11792E-06		
ROLLS	-.32677E-04	-.31941E-04	-.31478E-04	-.30355E-04	-.28791E-04	-.27671E-04		

TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2	
SSRU		35914E 00		36254E 00		45632E 00		45919E C0		54073E 00		54312E 07	
TIMES		-.34952E-01		-.35919E-01		-.73794E-01		-.75406E-C1		-.13647E 00		-.13374E 00	
XM		.92338E 02		.94281E 02		.15686E 03		.15906E 03		.22783E 03		.23003E 03	
YM		.35792E 01		.36490E 01		.57677E 01		.58409E 01		.78881E 01		.77470E 01	
PITCH		.25245E 01		.25019E 01		.17272E 01		.17027E C1		.12984E 01		.12562E 01	
YAW		-.25100E-01		-.26472E-01		-.77717E-01		-.77561E-01		-.79510E-01		-.77705E-01	
ROLL		-.34964E 04		-.35930E 04		-.39464E 04		-.39544E 04		-.46204E 04		-.4544E 04	
TIME		.57545E-05		-.11135E-03		.76441E-05		-.59125E-04		-.14069E-05		.16572E-04	
YAM		-.30874E-01		-.30967E-01		-.50912E-01		-.49467E-C1		-.65792E-01		-.63690E-01	
YIM		.53214E 02		.51505E 02		.57283E 02		.57255E 02		.59033E 02		.57011E 02	
OPITCH		.14232E 01		.17517E 01		.17904E 01		.17250E 01		.25559E 01		.14790E 01	
OYAW		-.66449E 00		-.64490E 00		-.44471E 00		-.42067E C0		.13109E 00		.13454E 00	
PDLL		-.43834E-01		-.42636E-01		-.23506E-01		-.21952E-C1		.36853E-01		.36384E-01	
PITCHS		-.36033E 03		-.35053E 03		-.54738E 03		-.53367E 03		-.70268E 03		-.68107E 03	
YAWS		-.14024E-07		.31373E-05		.20793E-07		.18732E-05		.53855E-07		.12200E-05	
CRUS		-.76638E-04		-.10348E-03		-.68067E-04		-.74056E-04		-.58341E-04		-.78549E-04	
RAVS		.45084E-07		-.73760E-06		.67842E-07		-.20065E-C6		.84190E-07		-.65643E-06	
ALTS		.14623E-05		.14762E-05		.12964E-05		.13050E-05		.11076E-05		.11129E-05	
ROLLS		.64477E-07		.91531E-07		.37070E-07		.54904E-07		.24291E-07		.34573E-07	
		-.24577E-04		-.23584E-04		-.17316E-04		-.18487E-04		-.14107E-04		-.13459E-04	

(CONTINUOUS)

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TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2	
GSND													
TIMES		.76925E 00	.77052E 00	.80847E 00	.80958E 00	.84327E 00	.84427E 00	.84327E 00	.84427E 00	.84327E 00	.84427E 00	.84327E 00	.84427E 00
AM		-.44303E 00	-.44527E 00	-.52747E 00	-.52975E 00	-.59250E 00	-.59477E 00	-.59250E 00	-.59477E 00	-.59250E 00	-.59477E 00	-.59250E 00	-.59477E 00
YM		.48255E 03	.49421E 03	.53489E 03	.53641E 03	.58342E 03	.58443E 03	.58342E 03	.58443E 03	.58342E 03	.58443E 03	.58342E 03	.58443E 03
ZM		.13951E 02	.13985E 02	.15023E 02	.15054E 02	.15967E 02	.15994E 02	.15967E 02	.15994E 02	.15967E 02	.15994E 02	.15967E 02	.15994E 02
PITCH		.10544E 01	.10495E 01	.10039E 01	.10106E 01	.11072E 01	.11105E 01	.11072E 01	.11105E 01	.11072E 01	.11105E 01	.11072E 01	.11105E 01
YAW		-.12213E 00	-.12280E 00	-.12562E 00	-.12569E 00	-.17692E 01	-.17507E 01	-.17692E 01	-.17507E 01	-.17692E 01	-.17507E 01	-.17692E 01	-.17507E 01
ROLL		-.85825E 04	-.86166E 04	-.97171E 04	-.97519E 04	-.10874E 05	-.10710E 05	-.10874E 05	-.10710E 05	-.10874E 05	-.10710E 05	-.10874E 05	-.10710E 05
DYMF		.12321E 05	-.23412E 05	-.13235E 05	.38633E 05	-.11901E 05	.25049E 05	-.11901E 05	.25049E 05	-.11901E 05	.25049E 05	-.11901E 05	.25049E 05
DXM		-.62505E 01	-.60405E 01	-.63203E 01	-.61076E 01	-.61892E 01	-.59775E 01	-.61892E 01	-.59775E 01	-.61892E 01	-.59775E 01	-.61892E 01	-.59775E 01
DYM		.44277E 02	.42719E 02	.42057E 02	.37637E 02	.38243E 02	.36713E 02	.38243E 02	.36713E 02	.38243E 02	.36713E 02	.38243E 02	.36713E 02
ZYM		.91145E 00	.87855E 00	.80185E 00	.77330E 00	.71612E 00	.69078E 00	.71612E 00	.69078E 00	.71612E 00	.69078E 00	.71612E 00	.69078E 00
DPITCH		-.52477E 01	-.47534E 01	.80838E 01	.79290E 01	.65544E 01	.62335E 01	.65544E 01	.62335E 01	.65544E 01	.62335E 01	.65544E 01	.62335E 01
DYAW		.12035E 02	.19240E 02	.33134E 01	.32287E 01	.24824E 01	.23521E 01	.24824E 01	.23521E 01	.24824E 01	.23521E 01	.24824E 01	.23521E 01
ROLL		-.95234E 03	-.92039E 03	-.97239E 03	-.94042E 03	-.78535E 03	-.75180E 03	-.78535E 03	-.75180E 03	-.78535E 03	-.75180E 03	-.78535E 03	-.75180E 03
PITCHS		.52950E 07	.54462E 06	.52231E 07	.40451E 06	.39398E 07	.43520E 05	.39398E 07	.43520E 05	.39398E 07	.43520E 05	.39398E 07	.43520E 05
YAWS		-.32076E 04	-.39270E 04	-.28502E 04	-.34224E 04	-.25616E 04	-.30212E 04	-.25616E 04	-.30212E 04	-.25616E 04	-.30212E 04	-.25616E 04	-.30212E 04
CADS		.96074E 07	-.30190E 06	.97076E 07	-.25745E 06	.91634E 07	-.22251E 05	.91634E 07	-.22251E 05	.91634E 07	-.22251E 05	.91634E 07	-.22251E 05
RAVS		.59705E 05	.59775E 05	.52748E 06	.52793E 06	.47131E 06	.47194E 05	.47131E 06	.47194E 05	.47131E 06	.47194E 05	.47131E 06	.47194E 05
ALTS		.10825E 07	.15130E 07	.91109E 08	.12802E 07	.59648E 08	.12358E 07	.59648E 08	.12358E 07	.59648E 08	.12358E 07	.59648E 08	.12358E 07
ROLLS		-.41068E 05	-.39365E 05	-.32066E 05	-.30761E 05	-.25613E 05	-.24596E 05	-.25613E 05	-.24596E 05	-.25613E 05	-.24596E 05	-.25613E 05	-.24596E 05

TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2	
CSNO													
TIMES		.87449E 00	.87540E 00	.87540E 00	.87540E 00	.90278E 00	.90361E 00	.90361E 00	.92865E 00	.92865E 00	.92865E 00	.92865E 00	.92865E 00
XM		-.56575E 00	-.66795E 00	-.66795E 00	-.66795E 00	-.73574E 00	-.73782E 00	-.73782E 00	-.80247E 00	-.80247E 00	-.80247E 00	-.80247E 00	-.80247E 00
YM		.52857E 03	.52990E 03	.52990E 03	.52990E 03	.57091E 03	.67206E 03	.67206E 03	.71072E 03	.71072E 03	.71072E 03	.71072E 03	.71072E 03
ZM		.16811E 02	.16835E 02	.16835E 02	.16835E 02	.17575E 02	.17598E 02	.17598E 02	.18275E 02	.18275E 02	.18275E 02	.18275E 02	.18275E 02
PITCH		.11771E 01	.11776E 01	.11776E 01	.11776E 01	.11382E 01	.11354E 01	.11354E 01	.10220E 01	.10220E 01	.10220E 01	.10220E 01	.10220E 01
YAW		-.50259E-01	-.50018E-01	-.50018E-01	-.50018E-01	-.50555E-01	-.52937E-01	-.52937E-01	-.10214E 00	-.10214E 00	-.10214E 00	-.10214E 00	-.10214E 00
ROLL		-.12067E 05	-.12081E 05	-.12081E 05	-.12081E 05	-.13212E 05	-.13247E 05	-.13247E 05	-.14371E 05	-.14371E 05	-.14371E 05	-.14371E 05	-.14371E 05
TIME		.31460E-05	-.10768E-05	-.10768E-05	-.10768E-05	.14715E-05	.30572E-05	.30572E-05	.26419E-05	.26419E-05	.26419E-05	.26419E-05	.26419E-05
DXM		-.59220E-01	-.57170E-01	-.57170E-01	-.57170E-01	-.56462E-01	-.54505E-01	-.54505E-01	-.54445E-01	-.54445E-01	-.54445E-01	-.54445E-01	-.54445E-01
DYM		.35782E 02	.34534E 02	.34534E 02	.34534E 02	.33647E 02	.32473E 02	.32473E 02	.31777E 02	.31777E 02	.31777E 02	.31777E 02	.31777E 02
DPM		.54872E 00	.62599E 00	.62599E 00	.62599E 00	.57374E 00	.57297E 00	.57297E 00	.54651E 00	.54651E 00	.54651E 00	.54651E 00	.54651E 00
DPITCH		-.25944E-01	-.26601E-01	-.26601E-01	-.26601E-01	-.95228E-01	-.93414E-01	-.93414E-01	-.10202E 00	-.10202E 00	-.10202E 00	-.10202E 00	-.10202E 00
DYAW		-.74661E-02	-.77594E-02	-.77594E-02	-.77594E-02	-.33054E-01	-.32209E-01	-.32209E-01	-.34766E-01	-.34766E-01	-.34766E-01	-.34766E-01	-.34766E-01
DROLL		-.28357E 03	-.25030E 03	-.25030E 03	-.25030E 03	-.97853E 03	-.74522E 03	-.74522E 03	-.97322E 03	-.97322E 03	-.97322E 03	-.97322E 03	-.97322E 03
PITCHS		.29790E-07	.40377E-05	.40377E-05	.40377E-05	.29758E-07	.35527E-06	.35527E-06	.36254E-07	.36254E-07	.36254E-07	.36254E-07	.36254E-07
YAWS		-.23263E-04	-.26770E-04	-.26770E-04	-.26770E-04	-.21340E-04	-.24323E-04	-.24323E-04	-.19745E-04	-.19745E-04	-.19745E-04	-.19745E-04	-.19745E-04
CROSS		.89183E-07	-.19452E-06	-.19452E-06	-.19452E-06	.86777E-07	-.17182E-06	-.17182E-06	.84561E-07	.84561E-07	.84561E-07	.84561E-07	.84561E-07
RAWS		.42551E-06	.42615E-06	.42615E-06	.42615E-06	.39807E-06	.38837E-06	.38837E-06	.35677E-06	.35677E-06	.35677E-06	.35677E-06	.35677E-06
ALTS		.85265E-08	.11570E-07	.11570E-07	.11570E-07	.75864E-08	.10205E-07	.10205E-07	.62090E-08	.62090E-08	.62090E-08	.62090E-08	.62090E-08
ROLLS		-.20901E-05	-.20075E-05	-.20075E-05	-.20075E-05	-.17385E-05	-.16709E-05	-.16709E-05	-.14703E-05	-.14703E-05	-.14703E-05	-.14703E-05	-.14703E-05



TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2		1		2	
GSN)																	
TIMES		.95243E 00	.95317E 00	.95317E 00	.95317E 00	.97456E 00	.97456E 00	.97520E 00	.97520E 00	.99515E 00	.99515E 00	.99515E 00	.99515E 00	.99515E 00	.99515E 00	.99515E 00	.99515E 00
XM		-.86695E 00	-.86695E 00	-.86695E 00	-.86695E 00	-.93004E 00	-.93004E 00	-.93193E 00	-.93193E 00	-.99300E 00	-.99300E 00	-.99300E 00	-.99300E 00	-.99300E 00	-.99300E 00	-.99300E 00	-.99300E 00
YM		.74801E 03	.74801E 03	.74801E 03	.74801E 03	.79354E 03	.79354E 03	.78454E 03	.78454E 03	.81731E 03	.81731E 03	.81731E 03	.81731E 03	.81731E 03	.81731E 03	.81731E 03	.81731E 03
ZM		.18919E 02	.18919E 02	.18919E 02	.18919E 02	.19913E 02	.19913E 02	.19530E 02	.19530E 02	.20002E 02	.20002E 02	.20002E 02	.20002E 02	.20002E 02	.20002E 02	.20002E 02	.20002E 02
PITCH		.90344E 00	.90344E 00	.90344E 00	.90344E 00	.83748E 00	.83748E 00	.83654E 00	.83654E 00	.83543E 00	.83543E 00	.83543E 00	.83543E 00	.83543E 00	.83543E 00	.83543E 00	.83543E 00
YAW		-.14197E 00	-.14197E 00	-.14197E 00	-.14197E 00	-.15796E 00	-.15796E 00	-.15796E 00	-.15796E 00	-.14434E 00	-.14434E 00	-.14434E 00	-.14434E 00	-.14434E 00	-.14434E 00	-.14434E 00	-.14434E 00
ROLL		-.15524E 05	-.15524E 05	-.15524E 05	-.15524E 05	-.16669E 05	-.16669E 05	-.16703E 05	-.16703E 05	-.17808E 05	-.17808E 05	-.17808E 05	-.17808E 05	-.17808E 05	-.17808E 05	-.17808E 05	-.17808E 05
DYMF		.99345E 05	.99345E 05	.99345E 05	.99345E 05	.14388E 06	.14388E 06	.33597E 07	.33597E 07	.42572E 06	.42572E 06	.42572E 06	.42572E 06	.42572E 06	.42572E 06	.42572E 06	.42572E 06
DXM		-.53405E 01	-.53405E 01	-.53405E 01	-.53405E 01	-.53194E 01	-.53194E 01	-.53993E 01	-.53993E 01	-.53457E 01	-.53457E 01	-.53457E 01	-.53457E 01	-.53457E 01	-.53457E 01	-.53457E 01	-.53457E 01
DYM		.30122E 02	.30122E 02	.30122E 02	.30122E 02	.28646E 02	.28646E 02	.27659E 02	.27659E 02	.27317E 02	.27317E 02	.27317E 02	.27317E 02	.27317E 02	.27317E 02	.27317E 02	.27317E 02
D/M		.50468E 00	.50468E 00	.50468E 00	.50468E 00	.46725E 00	.46725E 00	.45076E 00	.45076E 00	.43377E 00	.43377E 00	.43377E 00	.43377E 00	.43377E 00	.43377E 00	.43377E 00	.43377E 00
DPITCH		-.60117E 01	-.60117E 01	-.60117E 01	-.60117E 01	-.52577E 02	-.52577E 02	-.42830E 02	-.42830E 02	.31576E 01	.31576E 01	.31576E 01	.31576E 01	.31576E 01	.31576E 01	.31576E 01	.31576E 01
DYAW		-.15535E 01	-.15535E 01	-.15535E 01	-.15535E 01	.94703E 02	.94703E 02	.94097E 02	.94097E 02	.26571E 01	.26571E 01	.26571E 01	.26571E 01	.26571E 01	.26571E 01	.26571E 01	.26571E 01
DRULL		-.96785E 03	-.96785E 03	-.96785E 03	-.96785E 03	-.96253E 03	-.96253E 03	-.93003E 03	-.93003E 03	-.95671E 03	-.95671E 03	-.95671E 03	-.95671E 03	-.95671E 03	-.95671E 03	-.95671E 03	-.95671E 03
PITCHS		.42973E 07	.42973E 07	.42973E 07	.42973E 07	.45628E 07	.45628E 07	.23170E 06	.23170E 06	.43474E 07	.43474E 07	.43474E 07	.43474E 07	.43474E 07	.43474E 07	.43474E 07	.43474E 07
YAWS		-.19395E 04	-.19395E 04	-.19395E 04	-.19395E 04	-.17237E 04	-.17237E 04	-.21673E 04	-.21673E 04	-.16248E 04	-.16248E 04	-.16248E 04	-.16248E 04	-.16248E 04	-.16248E 04	-.16248E 04	-.16248E 04
CRDS		.82457E 07	.82457E 07	.82457E 07	.82457E 07	.80470E 07	.80470E 07	-.12442E 06	-.12442E 06	.78579E 07	.78579E 07	.78579E 07	.78579E 07	.78579E 07	.78579E 07	.78579E 07	.78579E 07
RANS		.33058E 06	.33058E 06	.33058E 06	.33058E 06	.30809E 06	.30809E 06	.30730E 06	.30730E 06	.28843E 06	.28843E 06	.28843E 06	.28843E 06	.28843E 06	.28843E 06	.28843E 06	.28843E 06
ALTS		.50159E 03	.50159E 03	.50159E 03	.50159E 03	.42851E 08	.42851E 08	.60203E 08	.60203E 08	.39905E 08	.39905E 08	.39905E 08	.39905E 08	.39905E 08	.39905E 08	.39905E 08	.39905E 08
ROLLS		-.12509E 05	-.12509E 05	-.12509E 05	-.12509E 05	-.10943E 05	-.10943E 05	-.10531E 05	-.10531E 05	-.95935E 06	-.95935E 06	-.95935E 06	-.95935E 06	-.95935E 06	-.95935E 06	-.95935E 06	-.95935E 06

TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2	
SSND													
TIMES		.10144E 01	.10150E 01	.10150E 01	.10150E 01	.10326E 01	.10331E 01	.10331E 01	.10497E 01	.10497E 01	.10502E 01	.10502E 01	.10502E 01
XY		-.10553E 01	-.10582E 01	-.10582E 01	-.10582E 01	-.11200E 01	-.11217E 01	-.11217E 01	-.11839E 01	-.11839E 01	-.11858E 01	-.11858E 01	-.11858E 01
YM		.84951E 03	.85046E 03	.85046E 03	.85046E 03	.84030E 03	.84121E 03	.84121E 03	.90981E 03	.90981E 03	.91069E 03	.91069E 03	.91069E 03
ZM		.20572E 02	.20587E 02	.20587E 02	.20587E 02	.21048E 02	.21061E 02	.21061E 02	.21492E 02	.21492E 02	.21505E 02	.21505E 02	.21505E 02
PITCH		.87425E 00	.87553E 00	.87553E 00	.87553E 00	.91859E 00	.91968E 00	.91968E 00	.93980E 00	.93980E 00	.93991E 00	.93991E 00	.93991E 00
YAW		-.11239E 00	-.11134E 00	-.11134E 00	-.11134E 00	-.91328E-01	-.80596E-01	-.80596E-01	-.67950E-01	-.67950E-01	-.57716E-01	-.57716E-01	-.57716E-01
ROLL		-.18939E 05	-.18972E 05	-.18972E 05	-.18972E 05	-.20053E 05	-.20097E 05	-.20097E 05	-.21153E 05	-.21153E 05	-.21195E 05	-.21195E 05	-.21195E 05
DTMF		-.54603E-06	.72993E-06	.72993E-06	.72993E-06	-.30461E-06	.32119E-06	.32119E-06	.10030E-06	.10030E-06	-.20454E-06	-.20454E-06	-.20454E-06
QAM		-.53977E-01	-.52075E-01	-.52075E-01	-.52075E-01	-.54094E-01	-.52279E-01	-.52279E-01	-.53734E-01	-.53734E-01	-.51766E-01	-.51766E-01	-.51766E-01
DYM		.26123E 02	.25233E 02	.25233E 02	.25233E 02	.25056E 02	.24199E 02	.24199E 02	.26065E 02	.26065E 02	.23941E 02	.23941E 02	.23941E 02
DZM		.40407E 00	.38999E 00	.38999E 00	.38999E 00	.37761E 00	.36453E 00	.36453E 00	.35433E 00	.35433E 00	.34207E 00	.34207E 00	.34207E 00
DPITCH		.38450E-01	.37102E-01	.37102E-01	.37102E-01	.20174E-01	.19097E-01	.19097E-01	-.10051E-01	-.10051E-01	-.10156E-01	-.10156E-01	-.10156E-01
DYAW		.27071E-01	.26791E-01	.26791E-01	.26791E-01	.11208E-01	.12194E-01	.12194E-01	-.03959E-02	-.03959E-02	-.84452E-02	-.84452E-02	-.84452E-02
DROLL		-.94415E 03	-.91225E 03	-.91225E 03	-.91225E 03	-.73133E 03	-.47986E 03	-.47986E 03	-.91963E 03	-.91963E 03	-.84452E 03	-.84452E 03	-.84452E 03
PITCHS		.38444E-07	.20599E-06	.20599E-06	.20599E-06	.33337E-07	.9781E-06	.9781E-06	.30126E-07	.30126E-07	.13410E-06	.13410E-06	.13410E-06
YAWS		-.15343E-04	-.16251E-04	-.16251E-04	-.16251E-04	-.14568E-04	.15248E-04	.15248E-04	-.13866E-04	-.13866E-04	-.14364E-04	-.14364E-04	-.14364E-04
CRDS		.76792E-07	-.10351E-05	-.10351E-05	-.10351E-05	.75142E-07	-.95248E-07	-.95248E-07	.73629E-07	.73629E-07	-.37915E-07	-.37915E-07	-.37915E-07
RANS		.27117E-06	.27098E-05	.27098E-05	.27098E-05	.25608E-06	.25560E-06	.25560E-06	.24279E-06	.24279E-06	.24232E-06	.24232E-06	.24232E-06
ALTS		.39421E-08	.54454E-08	.54454E-08	.54454E-08	.39314E-08	.53362E-08	.53362E-08	.38209E-08	.38209E-08	.51246E-08	.51246E-08	.51246E-08
ROLLS		-.84867E-06	-.81721E-06	-.81721E-06	-.81721E-06	-.75729E-06	-.72940E-06	-.72940E-06	-.68095E-06	-.68095E-06	-.65602E-06	-.65602E-06	-.65602E-06

TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2	
SSUJ		.10659E 01	.10664E 01	.10664E 01	.10813E 01	.10818E 01	.10818E 01	.10818E 01	.10818E 01	.10961E 01	.10961E 01	.10965E 01	.10965E 01
TIMES		-.12473E 01	-.12492E 01	-.12492E 01	-.13094E 01	-.13113E 01	-.13113E 01	-.13113E 01	-.13113E 01	-.13692E 01	-.13692E 01	-.13710E 01	-.13710E 01
XM		.93813E 03	.73902E 03	.73902E 03	.96549E 03	.96630E 03	.96630E 03	.96630E 03	.96630E 03	.99185E 03	.99185E 03	.79262E 03	.79262E 03
YM		.21904E 02	.21920E 02	.21920E 02	.22391E 02	.22312E 02	.22312E 02	.22312E 02	.22312E 02	.22673E 02	.22673E 02	.22584E 02	.22584E 02
PITCH		.92524E 00	.92423E 00	.92423E 00	.87841E 00	.87664E 00	.87664E 00	.87664E 00	.87664E 00	.81367E 00	.81367E 00	.41164E 00	.41164E 00
YAW		-.79749E-01	-.80491E-01	-.80491E-01	-.11318E 00	-.11440E 00	-.11440E 00	-.11440E 00	-.11440E 00	-.15562E 00	-.15562E 00	-.15751E 00	-.15751E 00
ROLL		-.22233E 05	-.22270E 05	-.22270E 05	-.23310E 05	-.23342E 05	-.23342E 05	-.23342E 05	-.23342E 05	-.24399E 05	-.24399E 05	-.24332E 05	-.24332E 05
DYME		.47637E-06	-.60497E-06	-.60497E-06	.62833E-06	.77050E-06	.77050E-06	.77050E-06	.77050E-06	.72246E-06	.72246E-06	-.70436E-06	-.70436E-06
DAM		-.52719E-01	-.59923E-01	-.59923E-01	-.59849E-01	-.49103E-01	-.49103E-01	-.49103E-01	-.49103E-01	-.48394E-01	-.48394E-01	-.46726E-01	-.46726E-01
DYM		.23202E 02	.22403E 02	.22403E 02	.21395E 02	.21628E 02	.21628E 02	.21628E 02	.21628E 02	.21607E 02	.21607E 02	.20917E 02	.20917E 02
DYV		.33401E 00	.32247E 00	.32247E 00	.31553E 00	.30562E 00	.30562E 00	.30562E 00	.30562E 00	.30193E 00	.30193E 00	.29154E 00	.29154E 00
PITCH		-.38058E-01	-.37157E-01	-.37157E-01	-.54426E-01	-.52758E-01	-.52758E-01	-.52758E-01	-.52758E-01	-.55547E-01	-.55547E-01	-.53608E-01	-.53608E-01
DYAW		-.27325E-01	-.26642E-01	-.26642E-01	-.36674E-01	-.35313E-01	-.35313E-01	-.35313E-01	-.35313E-01	-.32621E-01	-.32621E-01	-.31390E-01	-.31390E-01
OROLL		-.79890E 03	-.87814E 03	-.87814E 03	-.87120E 03	-.86074E 03	-.86074E 03	-.86074E 03	-.86074E 03	-.85271E 03	-.85271E 03	-.83316E 03	-.83316E 03
PITCHS		.29521E-07	.17621E-05	.17621E-05	.31480E-07	.16304E-06	.16304E-06	.16304E-06	.16304E-06	.34665E-07	.34665E-07	.15013E-05	.15013E-05
YAWs		-.13244E-04	-.13978E-04	-.13978E-04	-.12748E-04	-.12374E-04	-.12374E-04	-.12374E-04	-.12374E-04	-.12272E-04	-.12272E-04	-.12247E-04	-.12247E-04
CPDS		.72242E-07	-.81423E-07	-.81423E-07	.79671E-07	-.75649E-07	-.75649E-07	-.75649E-07	-.75649E-07	.69815E-07	.69815E-07	-.70479E-07	-.70479E-07
RAWS		.23102E-06	.23942E-06	.23942E-06	.21038E-06	.19711E-06	.19711E-06	.19711E-06	.19711E-06	.21120E-06	.21120E-06	.21013E-06	.21013E-06
ALTS		.35575E-08	.47716E-09	.47716E-09	.30028E-09	.45166E-09	.45166E-09	.45166E-09	.45166E-09	.17979E-08	.17979E-08	.38369E-08	.38369E-08
ROLLS		-.61642E-06	-.59395E-06	-.59395E-06	-.56130E-06	-.54097E-06	-.54097E-06	-.54097E-06	-.54097E-06	-.51425E-06	-.51425E-06	-.49574E-06	-.49574E-06



TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2	
SSN													
TIMES		.11491E 01	.11495E 01	.11495E 01	.11495E 01	.11512E 01	.11615E 01	.11615E 01	.11729E 01	.11732E 01			
XY		-.15818E 01	-.15833E 01	-.15833E 01	-.15833E 01	-.16336E 01	-.16352E 01	-.16352E 01	-.16891E 01	-.16908E 01			
YM		.10896E 04	.10901E 04	.10901E 04	.10901E 04	.11122E 04	.11122E 04	.11122E 04	.11344E 04	.11351E 04			
ZM		.24014E 02	.24023E 02	.24023E 02	.24023E 02	.24321E 02	.24330E 02	.24330E 02	.24610E 02	.24614E 02			
PITCH		.67997E 00	.68039E 00	.68039E 00	.68039E 00	.70538E 00	.70795E 00	.70795E 00	.74790E 00	.74792E 00			
YAW		-.17067E 00	-.16222E 00	-.16222E 00	-.16222E 00	-.12117E 00	-.12269E 00	-.12269E 00	-.70520E 01	-.69131E 01			
ROLL		-.28244E 05	-.28272E 05	-.28272E 05	-.28272E 05	-.29151E 05	-.29177E 05	-.29177E 05	-.30035E 05	-.30161E 05			
DIR		-.23789E 06	.25098E 06	.25098E 06	.25098E 06	-.39707E 06	.39502E 06	.39502E 06	-.43917E 06	.33375E 05			
DM		-.43327E 01	-.42386E 01	-.42386E 01	-.42386E 01	-.45818E 01	-.45302E 01	-.45302E 01	-.51569E 01	-.49244E 01			
DN		.19371E 02	.18715E 02	.18715E 02	.18715E 02	.14910E 02	.14271E 02	.14271E 02	.18431E 02	.17452E 02			
DZ		.26102E 00	.25222E 00	.25222E 00	.25222E 00	.29145E 00	.24897E 00	.24897E 00	.24059E 00	.23239E 00			
OPITCH		.21775E 01	.21304E 01	.21304E 01	.21304E 01	.34401E 01	.35334E 01	.35334E 01	.37053E 01	.35304E 01			
OYAW		.41436E 01	.40267E 01	.40267E 01	.40267E 01	.43624E 01	.42110E 01	.42110E 01	.31105E 01	.29500E 01			
OROLL		-.77117E 03	-.74503E 03	-.74503E 03	-.74503E 03	-.75299E 03	-.72707E 03	-.72707E 03	-.73507E 03	-.71910E 03			
PITCHS		.39595E 07	.11976E 06	.11976E 06	.11976E 06	.36909E 07	.11727E 06	.11727E 06	.33365E 07	.11518E 06			
YAWS		-.10812E 04	-.10361E 04	-.10361E 04	-.10361E 04	-.10523E 04	-.10001E 04	-.10001E 04	-.10258E 04	-.96732E 05			
CRYS		.65200E 07	-.54390E 07	-.54390E 07	-.54390E 07	.65453E 07	.51974E 07	.51974E 07	.64753E 07	-.49134E 07			
RLYS		.18235E 05	.18115E 05	.18115E 05	.18115E 05	.17660E 06	.17557E 06	.17557E 06	.17131E 06	.17049E 06			
ALTS		.19171E 03	.27814E 03	.27814E 03	.27814E 03	.19463E 03	.17750E 03	.17750E 03	.20241E 03	.20147E 03			
ROLLS		-.38312E 05	-.36957E 06	-.36957E 06	-.36957E 06	-.35979E 06	-.34710E 06	-.34710E 06	-.33903E 06	-.32711E 06			

TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2	
SSWJ													
TIMES		.11842E 01	.11946E 01	.11752E 01	.11956E 01	.12059E 01	.12059E 01	.12059E 01	.12059E 01	.12059E 01	.12059E 01	.12059E 01	.12059E 01
XY		-.17503E 01	-.17522E 01	-.18130E 01	-.18201E 01	-.18912E 01	-.18912E 01	-.18912E 01	-.18912E 01	-.18912E 01	-.18912E 01	-.18912E 01	-.18912E 01
YM		.11551E 04	.11563E 04	.11774E 04	.11780E 04	.11962E 04	.11962E 04	.11962E 04	.11962E 04	.11962E 04	.11962E 04	.11962E 04	.11962E 04
ZM		.24879E 01	.24906E 02	.25165E 02	.25173E 02	.25416E 02	.25416E 02	.25416E 02	.25416E 02	.25416E 02	.25416E 02	.25416E 02	.25416E 02
PITCH		.79110E 00	.79239E 00	.82419E 00	.82490E 00	.83619E 00	.83619E 00	.83619E 00	.83619E 00	.83619E 00	.83619E 00	.83619E 00	.83619E 00
YAW		-.35877E-01	-.35261E-01	-.32414E-01	-.32921E-01	-.32930E-01	-.32930E-01	-.32930E-01	-.32930E-01	-.32930E-01	-.32930E-01	-.32930E-01	-.32930E-01
ROLL		-.30328E 05	-.30226E 05	-.31743E 05	-.31763E 05	-.32567E 05	-.32567E 05	-.32567E 05	-.32567E 05	-.32567E 05	-.32567E 05	-.32567E 05	-.32567E 05
CMF		-.36134E-06	.22665E-06	-.17580E-06	.2305E-07	.96172E-07	.96172E-07	.96172E-07	.96172E-07	.96172E-07	.96172E-07	.96172E-07	.96172E-07
CMR		-.57153E-01	-.55327E-01	-.62059E-01	-.60047E-01	-.64340E-01	-.64340E-01	-.64340E-01	-.64340E-01	-.64340E-01	-.64340E-01	-.64340E-01	-.64340E-01
DM		.24035E 02	.17475E 02	.17716E 02	.17119E 02	.17371E 02	.17371E 02	.17371E 02	.17371E 02	.17371E 02	.17371E 02	.17371E 02	.17371E 02
DM		.22529E 00	.22065E 00	.21457E 00	.20712E 00	.20017E 00	.20017E 00	.20017E 00	.20017E 00	.20017E 00	.20017E 00	.20017E 00	.20017E 00
PITCH		.27222E-01	.24070E-01	.18920E-01	.11147E-01	.2792E-01	.2792E-01	.2792E-01	.2792E-01	.2792E-01	.2792E-01	.2792E-01	.2792E-01
YAW		.53625E-02	.47437E-02	-.28712E-01	-.28236E-01	-.63453E-01	-.63453E-01	-.63453E-01	-.63453E-01	-.63453E-01	-.63453E-01	-.63453E-01	-.63453E-01
ROLL		-.71433E 03	-.67653E 03	-.70363E 03	-.67234E 03	-.68936E 03	-.68936E 03	-.68936E 03	-.68936E 03	-.68936E 03	-.68936E 03	-.68936E 03	-.68936E 03
PITCH		.29732E-07	.11404E-06	.26743E-07	.11193E-06	.35204E-07	.35204E-07	.35204E-07	.35204E-07	.35204E-07	.35204E-07	.35204E-07	.35204E-07
YAW		-.10015E-06	-.92623E-05	-.97791E-05	-.90862E-05	-.96020E-05	-.96020E-05	-.96020E-05	-.96020E-05	-.96020E-05	-.96020E-05	-.96020E-05	-.96020E-05
CROSS		.64130E-07	-.46542E-07	.63587E-07	-.44156E-07	.63115E-07	.63115E-07	.63115E-07	.63115E-07	.63115E-07	.63115E-07	.63115E-07	.63115E-07
ROLL		.16549E-06	.12575E-05	.19208E-06	.16134E-06	.25308E-06	.25308E-06	.25308E-06	.25308E-06	.25308E-06	.25308E-06	.25308E-06	.25308E-06
ALTS		.21074E-03	.28580E-04	.21570E-03	.28661E-03	.21372E-03	.21372E-03	.21372E-03	.21372E-03	.21372E-03	.21372E-03	.21372E-03	.21372E-03
ROLLS		-.32045E-05	-.30921E-05	-.30374E-06	-.29311E-06	-.28864E-06	-.28864E-06	-.28864E-06	-.28864E-06	-.28864E-06	-.28864E-06	-.28864E-06	-.28864E-06

TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2	
SSN7		.12163E 01	.12167E 01	.12265E 01	.12263E 01	.22304E 01	.22304E 01	.12263E 01	.22304E 01	.22304E 01	.12263E 01	.22304E 01	.12263E 01
TIMES		-.19668E 01	-.19690E 01	-.20390E 01	-.20410E 01	-.21004E 01	-.21004E 01	-.20410E 01	-.21004E 01	-.21004E 01	-.20410E 01	-.21004E 01	-.21004E 01
XM		.12196E 04	.12192E 04	.12396E 04	.12391E 04	.12544E 04	.12544E 04	.12391E 04	.12544E 04	.12544E 04	.12391E 04	.12544E 04	.12544E 04
YM		.25650E 02	.25557E 02	.25468E 02	.25474E 02	.26073E 02	.26073E 02	.25474E 02	.26073E 02	.26073E 02	.25474E 02	.26073E 02	.26073E 02
PITCH		.81873E 01	.81769E 00	.76722E 00	.76515E 00	.68161E 00	.68161E 00	.76515E 00	.68161E 00	.68161E 00	.76515E 00	.68161E 00	.68161E 00
YAW		-.14654E 00	-.14939E 00	-.25302E 00	-.25645E 00	-.36688E 00	-.36688E 00	-.25645E 00	-.36688E 00	-.36688E 00	-.25645E 00	-.36688E 00	-.36688E 00
ROLL		-.33378E 05	-.33402E 05	-.34172E 05	-.34195E 05	-.34295E 05	-.34295E 05	-.34195E 05	-.34295E 05	-.34295E 05	-.34195E 05	-.34295E 05	-.34295E 05
TIME		.42473E-03	-.35213E-05	.77152E-06	-.52495E-06	.10819E-05	.10819E-05	-.52495E-06	.10819E-05	.10819E-05	-.52495E-06	.10819E-05	.10819E-05
DXM		-.61964E-01	-.59317E-01	-.53287E-01	-.51323E-01	-.37670E-01	-.37670E-01	-.51323E-01	-.37670E-01	-.37670E-01	-.51323E-01	-.37670E-01	-.37670E-01
DYM		.17048E 02	.16471E 02	.16744E 02	.16177E 02	.16457E 02	.16457E 02	.16177E 02	.16457E 02	.16457E 02	.16177E 02	.16457E 02	.16457E 02
DYM		.18633E 00	.17783E 00	.17484E 00	.16982E 00	.16807E 00	.16807E 00	.16982E 00	.16807E 00	.16807E 00	.16982E 00	.16807E 00	.16807E 00
PITCH		-.41581E-01	-.40537E-01	-.70562E-01	-.58722E-01	-.75879E-01	-.75879E-01	-.58722E-01	-.75879E-01	-.75879E-01	-.58722E-01	-.75879E-01	-.75879E-01
YAW		-.89504E-01	-.86315E-01	-.97624E-01	-.94349E-01	-.80039E-01	-.80039E-01	-.94349E-01	-.80039E-01	-.80039E-01	-.94349E-01	-.80039E-01	-.80039E-01
ROLL		-.67643E 03	-.65357E 03	-.66402E 03	-.64159E 03	-.65239E 03	-.65239E 03	-.64159E 03	-.65239E 03	-.65239E 03	-.64159E 03	-.65239E 03	-.65239E 03
PITCHS		.25545E-07	.10467E-05	.24157E-07	.74466E-07	.33139E-07	.33139E-07	.74466E-07	.33139E-07	.33139E-07	.74466E-07	.33139E-07	.33139E-07
YAWs		-.74267E-05	-.95713E-05	-.97675E-05	-.83379E-05	-.9124E-05	-.9124E-05	-.83379E-05	-.9124E-05	-.9124E-05	-.83379E-05	-.9124E-05	-.9124E-05
ROLLS		.62713E-07	-.39334E-07	.62373E-07	-.37874E-07	.6207E-07	.6207E-07	-.37874E-07	.6207E-07	.6207E-07	-.37874E-07	.6207E-07	.6207E-07
YAWs		.15445E-06	.15323E-06	.15114E-06	.14922E-06	.14807E-06	.14807E-06	.14922E-06	.14807E-06	.14807E-06	.14922E-06	.14807E-06	.14807E-06
ROLLS		.20337E-08	.26701E-08	.14288E-08	.24430E-08	.15279E-08	.15279E-08	.24430E-08	.15279E-08	.15279E-08	.24430E-08	.15279E-08	.15279E-08
ROLLS		-.27492E-05	-.26535E-06	-.26242E-06	-.25330E-06	-.25077E-06	-.25077E-06	-.25330E-06	-.25077E-06	-.25077E-06	-.25330E-06	-.25077E-06	-.25077E-06

TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2	
GSNC		1		2		1		2		1		2	
TIMPS		12450E 01	12463E 01	12555E 01	1258E 01	12647E 01	12650E 01	12647E 01	12650E 01	12647E 01	12650E 01	12647E 01	12650E 01
XM		21427E 01	21433E 01	21578E 01	21592E 01	21432E 01	21432E 01	21432E 01	21432E 01	21432E 01	21432E 01	21432E 01	21432E 01
YM		12775E 04	12780E 04	12905E 04	12970E 04	13151E 04	13156E 04	13151E 04	13156E 04	13151E 04	13156E 04	13151E 04	13156E 04
ZM		25270E 02	26276E 02	26468E 02	6374E 02	26600E 02	26607E 02	26600E 02	26607E 02	26600E 02	26607E 02	26600E 02	26607E 02
PITCH		56742E 00	56370E 00	43636E 00	6327E 00	3024E 00	3024E 00	3024E 00	3024E 00	3024E 00	3024E 00	3024E 00	3024E 00
YAW		45759E 00	45750E 00	44746E 00	48761E 00	4304E 00	4304E 00	4304E 00	4304E 00	4304E 00	4304E 00	4304E 00	4304E 00
ROLL		35716E 05	35739E 05	36471E 05	36491E 05	3724E 05	3724E 05	3724E 05	3724E 05	3724E 05	3724E 05	3724E 05	3724E 05
TIME		12830E-05	64214E-06	12388E-05	5772E-06	10035E-05	3544E-06	10035E-05	3544E-06	10035E-05	3544E-06	10035E-05	3544E-06
DXM		16223E-01	15351E-01	7580E-02	7543E-02	7602E-01	2714E-01	7602E-01	2714E-01	7602E-01	2714E-01	7602E-01	2714E-01
DYM		16185E 02	15636E 02	15722E 02	1580E 02	1564E 02	1514E 02	1564E 02	1514E 02	1564E 02	1514E 02	1564E 02	1514E 02
DZM		1667E 00	16307E 00	1722E 00	1734E 00	2013E 00	1264E 00	2013E 00	1264E 00	2013E 00	1264E 00	2013E 00	1264E 00
PPITCH		11073E 00	1073E 00	10721E 00	0532E 00	9313E-01	7772E-01	9313E-01	7772E-01	9313E-01	7772E-01	9313E-01	7772E-01
DYAW		32502E-01	30524E-01	43716E-01	45524E-01	1410E 00	1315E 00	1410E 00	1315E 00	1410E 00	1315E 00	1410E 00	1315E 00
DROLL		64377E 03	62205E 03	66217E 03	62053E 03	6407E 03	5125E 03	6407E 03	5125E 03	6407E 03	5125E 03	6407E 03	5125E 03
PITCHS		40176E-07	87214E-07	44461E-07	9116E-07	5651E-07	7504E-07	5651E-07	7504E-07	5651E-07	7504E-07	5651E-07	7504E-07
YAWs		82330E-05	77153E-05	85446E-05	7727E-05	8694E-05	7501E-06	8694E-05	7501E-06	8694E-05	7501E-06	8694E-05	7501E-06
CRDS		61776E-07	34327E-07	61442E-07	3272E-07	6103E-07	3126E-07	6103E-07	3126E-07	6103E-07	3126E-07	6103E-07	3126E-07
RAWS		14515E-06	14291E-06	14227E-06	1398E-06	13930E-06	1317E-06	13930E-06	1317E-06	13930E-06	1317E-06	13930E-06	1317E-06
ALTS		11511E-08	17733E-08	73740E-09	13892E-08	34857E-09	1901E-08	34857E-09	1901E-08	34857E-09	1901E-08	34857E-09	1901E-08
ROLLS		24043E-06	23210E-06	23060E-06	2263E-06	22146E-06	2132E-06	22146E-06	2132E-06	22146E-06	2132E-06	22146E-06	2132E-06





TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2	
SSND													
TIMES													
XW		.12977E 01	.13000E 01	.13000E 01	.13043E 01	.13161E 01	.13164E 01	.13043E 01	.13161E 01	.13161E 01	.13164E 01	.13043E 01	.13164E 01
YM		-.21061E 01	-.21092E 01	-.21092E 01	-.22789E 01	-.26357E 01	-.26357E 01	-.22789E 01	-.26357E 01	-.26357E 01	-.26357E 01	-.22789E 01	-.26357E 01
YN		.13869E 04	.13873E 04	.13873E 04	.14040E 04	.14210E 04	.14210E 04	.14040E 04	.14210E 04	.14210E 04	.14210E 04	.14040E 04	.14210E 04
ZN		.27206E 02	.27215E 02	.27215E 02	.28307E 02	.28687E 02	.28687E 02	.28307E 02	.28687E 02	.28687E 02	.28687E 02	.28307E 02	.28687E 02
PITCH		.55163E 00	.56204E 00	.56204E 00	.10188E 01	.17009E 01	.17009E 01	.10188E 01	.17009E 01	.17009E 01	.17009E 01	.10188E 01	.17009E 01
YAW		.85230E 00	.86434E 00	.86434E 00	.11778E 01	.13105E 01	.13105E 01	.11778E 01	.13105E 01	.13105E 01	.13105E 01	.11778E 01	.13105E 01
ROLL		-.40217E 05	-.40241E 05	-.40241E 05	-.40763E 05	-.41704E 05	-.41704E 05	-.40763E 05	-.41704E 05	-.41704E 05	-.41704E 05	-.40763E 05	-.41704E 05
STMF		-.37457E -05	.20745E -05	.20745E -05	-.57756E -05	.62466E -05	.62466E -05	-.57756E -05	.62466E -05	.62466E -05	.62466E -05	-.57756E -05	.62466E -05
DXM		-.13773E 00	-.13459E 00	-.13459E 00	-.29015E 00	-.28355E 00	-.28355E 00	-.29015E 00	-.28355E 00	-.28355E 00	-.28355E 00	-.29015E 00	-.28355E 00
DYM		.14676E 02	.14215E 02	.14215E 02	.14473E 02	.14007E 02	.14007E 02	.14473E 02	.14007E 02	.14007E 02	.14007E 02	.14473E 02	.14007E 02
DZN		.44374E 00	.33303E 00	.33303E 00	.32830E 00	.31721E 00	.31721E 00	.32830E 00	.31721E 00	.31721E 00	.31721E 00	.32830E 00	.31721E 00
DPITCH		.39431E 00	.37455E 00	.37455E 00	.57466E 00	.55677E 00	.55677E 00	.57466E 00	.55677E 00	.55677E 00	.55677E 00	.57466E 00	.55677E 00
DYAW		.30635E 00	.29484E 00	.29484E 00	.17705E 00	.16960E 00	.16960E 00	.17705E 00	.16960E 00	.16960E 00	.16960E 00	.17705E 00	.16960E 00
DROLL		-.63417E 03	-.61357E 03	-.61357E 03	-.63228E 03	-.63033E 03	-.63033E 03	-.63228E 03	-.63033E 03	-.63033E 03	-.63033E 03	-.63228E 03	-.63033E 03
PITCHS		.39820E -07	.80297E -07	.80297E -07	.15988E -07	.29730E -07	.29730E -07	.15988E -07	.29730E -07	.29730E -07	.29730E -07	.15988E -07	.29730E -07
YAWs		-.30327E -05	-.67715E -05	-.67715E -05	-.78762E -05	-.68640E -05	-.68640E -05	-.78762E -05	-.68640E -05	-.68640E -05	-.68640E -05	-.78762E -05	-.68640E -05
CRDS		.58371E -07	-.26129E -07	-.26129E -07	.57675E -07	-.24976E -07	-.24976E -07	.57675E -07	-.24976E -07	-.24976E -07	-.24976E -07	.57675E -07	-.24976E -07
RAWS		.12634E -06	.12810E -06	.12810E -06	.12333E -06	.22605E -06	.22605E -06	.12333E -06	.22605E -06	.22605E -06	.22605E -06	.12333E -06	.22605E -06
ALTS		.94465E -04	.15747E -04	.15747E -04	.21330E -04	.26420E -04	.26420E -04	.21330E -04	.26420E -04	.26420E -04	.26420E -04	.21330E -04	.26420E -04
ROLLS		-.18967E -06	-.18318E -06	-.18318E -06	-.18235E -06	-.17654E -06	-.17654E -06	-.18235E -06	-.17654E -06	-.17654E -06	-.17654E -06	-.18235E -06	-.17654E -06

TABLE 3 VARIATIONS AND SENSITIVITIES OF SKEWED SYSTEM  
(CONTINUED)

(CONTINUOUS)		1		2		1		2		1		2	
GSNO		1	2	1	2	1	2	1	2	1	2	1	2
TIMES		.13241E 01	.13244E 01	.14319E 01	.13322E 01	.13396E 01	.13399E 01	.13396E 01	.13399E 01	.13396E 01	.13399E 01	.13396E 01	.13399E 01
YM		-.32242E 01	-.32482E 01	-.40508E 01	-.40835E 01	-.50354E 01	-.50723E 01	-.50354E 01	-.50723E 01	-.50354E 01	-.50723E 01	-.50354E 01	-.50723E 01
YM		.14377E 04	.14382E 04	.14542E 04	.14547E 04	.14704E 04	.14710E 04	.14704E 04	.14710E 04	.14704E 04	.14710E 04	.14704E 04	.14710E 04
ZM		.28947E 02	.28954E 02	.28947E 02	.28949E 02	.28949E 02	.28949E 02	.28949E 02	.28949E 02	.28949E 02	.28949E 02	.28949E 02	.28949E 02
PITCH		.25341E 01	.26152E 01	.35187E 01	.35493E 01	.42400E 01	.42555E 01	.42400E 01	.42555E 01	.42400E 01	.42555E 01	.42400E 01	.42555E 01
YAW		.97706E 00	.95487E 00	-.41649E-01	-.3319E-01	-.19837E 01	-.20737E 01	-.19837E 01	-.20737E 01	-.19837E 01	-.20737E 01	-.19837E 01	-.20737E 01
ROLL		-.42443E 05	-.42433E 05	-.43179E 05	-.43187E 05	-.43859E 05	-.43859E 05	-.43859E 05	-.43859E 05	-.43859E 05	-.43859E 05	-.43859E 05	-.43859E 05
DIR		-.95255E-05	.20007E-05	-.10186E-04	-.74918E-06	-.69040E-05	-.45659E-05	-.69040E-05	-.45659E-05	-.69040E-05	-.45659E-05	-.69040E-05	-.45659E-05
UXM		-.59234E 00	-.67447E 00	-.83257E 00	-.81470E 00	-.40262E 00	-.77127E 00	-.40262E 00	-.77127E 00	-.40262E 00	-.77127E 00	-.40262E 00	-.77127E 00
YVM		.14079E 02	.13632E 02	.13923E 02	.13477E 02	.13825E 02	.13344E 02	.13825E 02	.13344E 02	.13825E 02	.13344E 02	.13825E 02	.13344E 02
ZM		.21553E-01	.16085E-01	-.36433E 00	-.36183E 00	-.95704E 00	-.94132E 00	-.95704E 00	-.94132E 00	-.95704E 00	-.94132E 00	-.95704E 00	-.94132E 00
DPITCH		.80267E 00	.77734E 00	.64542E 00	.62002E 00	.97419E-01	.75142E-01	.97419E-01	.75142E-01	.97419E-01	.75142E-01	.97419E-01	.75142E-01
YAW		-.81817E 00	-.80404E 00	-.15977E 01	-.15540E 01	-.25236E 01	-.24512E 01	-.25236E 01	-.24512E 01	-.25236E 01	-.24512E 01	-.25236E 01	-.24512E 01
ROLL		-.55405E 03	-.56403E 03	-.53917E 03	-.57138E 03	-.67892E 03	-.68212E 03	-.67892E 03	-.68212E 03	-.67892E 03	-.68212E 03	-.67892E 03	-.68212E 03
PITCHS		-.85351E-07	.12503E-06	-.15563E-06	.13296E-06	-.23586E-06	.17241E-06	-.23586E-06	.17241E-06	-.23586E-06	.17241E-06	-.23586E-06	.17241E-06
YAWS		-.76864E-05	-.65743E-05	-.77113E-05	-.63965E-05	-.78944E-05	-.60001E-05	-.78944E-05	-.60001E-05	-.78944E-05	-.60001E-05	-.78944E-05	-.60001E-05
CRDS		.57152E-07	-.22526E-07	.57749E-07	-.21365E-07	.59509E-07	-.20182E-07	.59509E-07	-.20182E-07	.59509E-07	-.20182E-07	.59509E-07	-.20182E-07
RAWS		.11929E-06	.12127E-06	.11913E-06	.11812E-06	.12141E-06	.11489E-06	.12141E-06	.11489E-06	.12141E-06	.11489E-06	.12141E-06	.11489E-06
ALTS		.60335E-08	.57892E-08	.84201E-08	.77694E-08	.10747E-07	.82026E-08	.10747E-07	.82026E-08	.10747E-07	.82026E-08	.10747E-07	.82026E-08
ROLLS		-.17045E-06	-.15483E-06	-.15491E-06	-.15933E-06	-.16025E-06	-.15430E-06	-.16025E-06	-.15430E-06	-.16025E-06	-.15430E-06	-.16025E-06	-.15430E-06

TABLE 4  
PRODUCTS OF SENSITIVITY AND VARIATION

(a) <u>Straight System</u>		10	100	500	800	1000	1200	1500
Downrange								
Roll	.4E-07	.1E-06	.7E-08	.2E-08	.7E-09	.4E-09	.5E-08	
Altitude	.1E-10	.3E-10	.3E-11	.4E-07	.4E-12	.1E-12	.1E-09	
Range	.1E-07	.3E-07	.1E-08	.2E-09	.2E-09	.1E-09	.2E-08	
Crossrange	.2E-11	.1E-10	.2E-11	.4E-12	.3E-12	.3E-12	.1E-09	
Yaw	.5E-11	.4E-09	.1E-10	.6E-11	.4E-11	.1E-10	.5E-08	
Pitch	.4E-08	.4E-06	.2E-08	.6E-09	.1E-08	.4E-10	.4E-07	

TABLE 4 (cont.)  
PRODUCTS OF SENSITIVITY AND VARIATION

(b) Skewed System		10	100	500	800	1000	1200	1500
Downrange								
Roll	.15E-02	.7E-01	.4E-02	.1E-02	.4E-03	.2E-03	.1E-03	
Altitude	.27E-07	.2E-06	.2E-07	.2E-08	.1E-08	.4E-09	.1E-07	
Range	.10E-05	.7E-03	.2E-04	.1E-04	.4E-05	.3E-05	.1E-05	
Crossrange	.10E-15	.3E-07	.2E-07	.1E-07	.4E-08	.2E-07	.2E-07	
Yaw	.20E-08	.4E-05	.8E-07	.2E-06	.3E-06	.5E-06	.1E-04	
Pitch	.10E-22	.2E-05	.2E-07	.1E-08	.5E-08	.1E-08	.1E-07	

## EXPERIMENTAL PROGRAM

(a) Description of the Experiment

The objective of the experimental program was to verify the system concept, in particular the mathematical formulation developed in the previous sections. It might be expected that problem areas not identified in the mathematical studies and earlier concept studies could be uncovered and investigated using the experimental apparatus.

Two static laser ground stations were fabricated, in addition to a model rocket equipped with two, 90° roof prisms. The ground stations were located on a line  $x = 30$  ft. crossrange, and the rocket was systematically positioned at various  $y$  and  $z$  coordinates along the line  $x = 0$  in the earth fixed system.

Each ground station incorporated a 3mw helium-neon laser operating at 6328 Å,\* a spatial filter and collimator. A mounting ring for the photodetectors was fixed to the collimator. Two holes were drilled through the ring and the photodetectors were inserted from the back and epoxied in place (see Figure 18). No auxiliary optics were used in the detection system since it was found that an adequate signal was obtained without this complication. A simple amplifier for the signal from the photodetectors was housed in a small aluminum chassis box which was epoxied to the top of the laser.

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\*Metrogic Model 420 Laser

The model rocket consisted of a short, heavy-walled, aluminum cylinder. At one axial position, two holes were bored through the wall of the cylinder. These holes were separated circumferentially by ninety degrees. One hole accommodated a mount for a straight reflector, and the other one accommodated a mount for a skewed reflector, allowing the angle  $\gamma$  for the reflector to be adjusted to a particular value prior to conducting the experiment. The details of the design of the rocket may be seen in Figure 19.

A steel drive shaft was attached to the back of the cylinder along the axis of the cylinder. The shaft was supported in cantilever fashion, with two ball bearings which were mounted in bearing blocks which were in turn attached to a base plate. An electric gear motor (9.61 rpm) was attached to the base plate and coupled to the drive shaft through a flexible coupling (see Figure 20).

Both lasers were mounted on heavy duty metal tripods to facilitate positioning and alignment. The model rocket was mounted on an L-bracket which was in turn attached to a rotary table. This arrangement provides a rather crude but rigid elevation over azimuth mount for the model.

In order to measure the various time intervals, two digital timers were used.\* The output signals of the photodetectors were amplified in the amplifier located on top of each laser. The outputs of these amplifiers were used as inputs to the timers to initiate and terminate counting. A schematic representation of the detection/timing circuit is shown in

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\*Universal Timer Model 7370  
Hewlett Packard Timer Model 523DR

Figure 21. The detection/timing circuit was used to make three different types of measurements. Roll rate was measured using a signal from one laser ground station. The time interval for one complete revolution of the rocket was measured by starting and stopping the counter with consecutive pulses from a single photodetector. This measurement was checked with a nearly instantaneous measurement of the roll rate which was obtained by starting the counter with a pulse from a photodetector located in the mounting ring on top of the collimator, and stopping the counter with a pulse from a detector located in the same mounting ring directly below the center of the collimator. The time interval between return pulses to the two laser stations from the straight reflector was measured by starting the counter with the pulse received at station 1, and stopping the counter with the return pulse received at station 2. Simultaneously the time interval between pulse receptions from the straight and skewed reflectors at station 1 was measured. The same pulse which initiated counting in the previous measurement initiated counting on the second counter. This count was stopped however by a return pulse from the skewed reflector received at station 1.

It is apparent that with only two counters available, all three intervals of interest could not be measured simultaneously. In view of the fact that the gear motor is synchronous, and therefore the roll rate would only change with the line frequency, the roll rate was measured separately and assumed to remain constant. Although this seems to be a reasonable assumption, it has been found that significant frequency fluctuations occur in the service provided by the University



Power House. Therefore, the roll rate was measured before and after each attitude determination to check for constant roll rate.

(b) Results of the Experimental Program

Setting the angle  $\gamma$  and measuring the various angles to a high degree of accuracy ultimately required the use of lasers and large optical levers. The entire system including ground stations, model, and retro-reflectors were eventually aligned to an angular accuracy of  $.05^\circ$ . Experiments were conducted with the model located at two different positions downrange and pitch and yaw attitudes varying from  $-20$  to  $+20$  degrees.

The measured time intervals were used to determine the pitch and yaw attitude using a Newton-Raphson technique as mentioned in the section entitled "Mathematical Description of the System". These tests indicate that, for the static system, the pitch and yaw can be determined to essentially the same accuracy as the experimental error associated with aligning the various components. Two demonstrations of this bench top system were conducted for army personnel.

## CONCLUSIONS

In general, it may be concluded that both the analytical and experimental investigations of the skewed retroreflector two ground station system made to date indicate that such a system could be a useful range instrumentation technique. The analytical studies indicate that the pitch error due to dynamics in the short range area arises from roll rate and range errors introduced into the  $\Delta t_{12}$  equation. In this region the pitch and yaw solutions are weakly coupled and as a result the yaw solution remains quite good. Throughout the midrange region the solution for both pitch and yaw appear to be accurate to within a tenth of a degree which could be adequate for range instrumentation. At the extreme downrange position, yaw and pitch solutions are more strongly coupled and large errors in both pitch and yaw are encountered which would be inadequate for a range instrumentation system. This phenomenon was, however, due to an error in the simulation which caused the rocket to experience extremely large pitch and yaw rates ( $1500^\circ/\text{sec}$ ) in the neighborhood of 1500 ft. downrange. These rates are unrealistically high.

It should be pointed out that while almost all aspects of the ARROW vehicle simulation are quite typical of tactical missiles and rockets which would be tested, the extremely large roll acceleration throughout the trajectory is atypical. Since the roll error is significant in both  $\Delta t$  equations, it is anticipated that the error terms would typically be smaller than those presented here. It is therefore concluded that the indicated degradation of system performance at 1500 ft. downrange is not the result of an actual system limitation but rather the unrealistically

high angular rates generated in the simulation.

Considerations such as ground station position optimization, retro-reflector geometry optimization, and alternate methods of data analysis have not been addressed. Further, work in these areas could be expected to produce a more accurate system.

One limitation not pointed out previously is the fact that the 1500 feet range represents a maximum for retroreflection from the skewed reflector to ground station number 1. It is now apparent that somewhere near midrange an equation for  $\Delta t_{22}$  should have been substituted for  $\Delta t_{11}$  which could have allowed data reduction out to 2000 feet and could possibly result in improved pitch and yaw solutions between 1300 feet and 2000 feet downrange. It should be noted that the yaw accuracy obtained is better than that associated with a similar system employing three ground stations and one single plane corner reflector onboard the vehicle<sup>(3)</sup>.

In summary, the two station concept offers all of the advantages originally anticipated for the three station system with the additional economic advantage of eliminating one ground station. It appears that yaw accuracy will be better than that associated with the three station system. Additional study covering ground station position optimization, retroreflector geometry optimization, and data analysis solutions are all required prior to implementing the concept as a range instrumentation technique.

## REFERENCES

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2. Mermagen, W.H. and Clay, W.H., "The Design of a Second Generation Yawsonde", BRL Memorandum Report No. 2368, April 1974.
3. Pell, K.M., Russell, J.J., Nydahl, J.E. and Lindberg, W.R., "A Laser System for Determination of Rocket Attitude and Roll Rate", UWME-DR-4061051, July 1974.
4. Harris, J.L., "Integrated System Simulation Development, A Six Degree of Freedom Rigid Body Simulation", U.S. Army Missile Command, RD-TR-69-3.

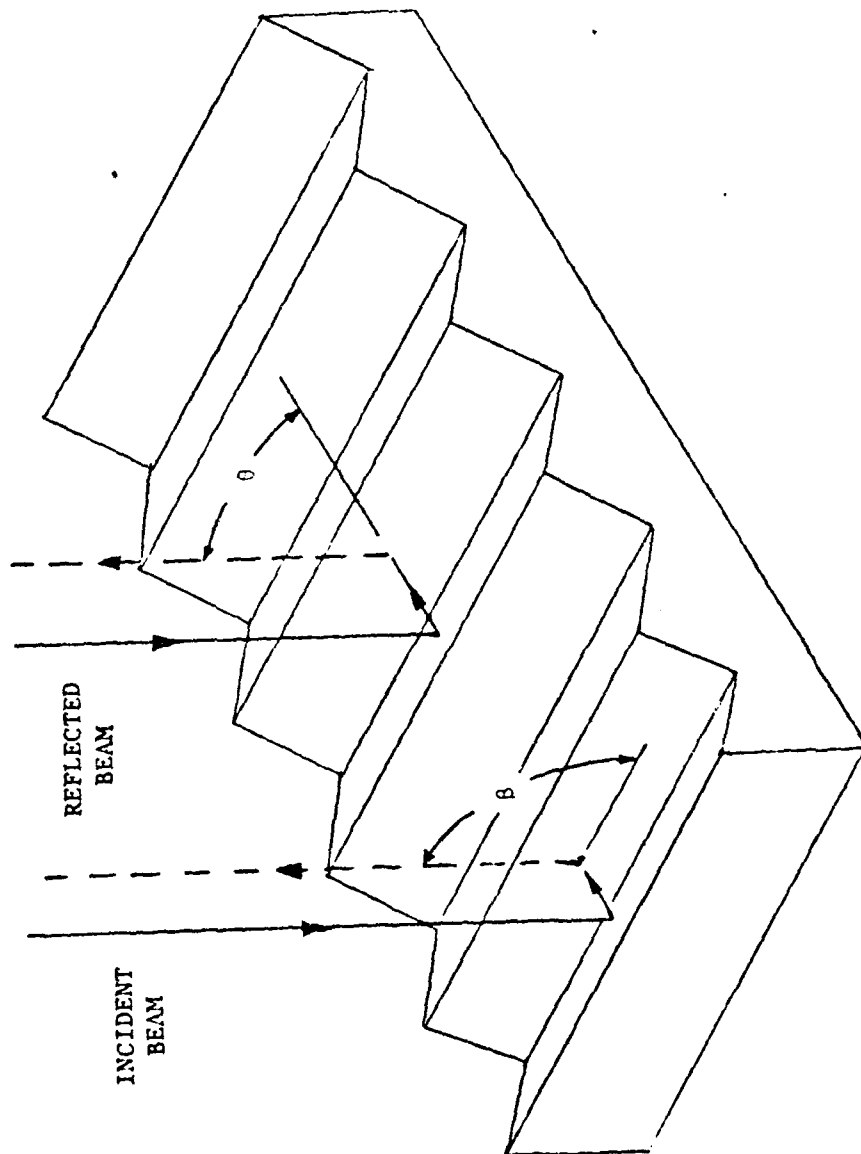


FIGURE 1 - SINGLE PLANE CORNER REFLECTOR

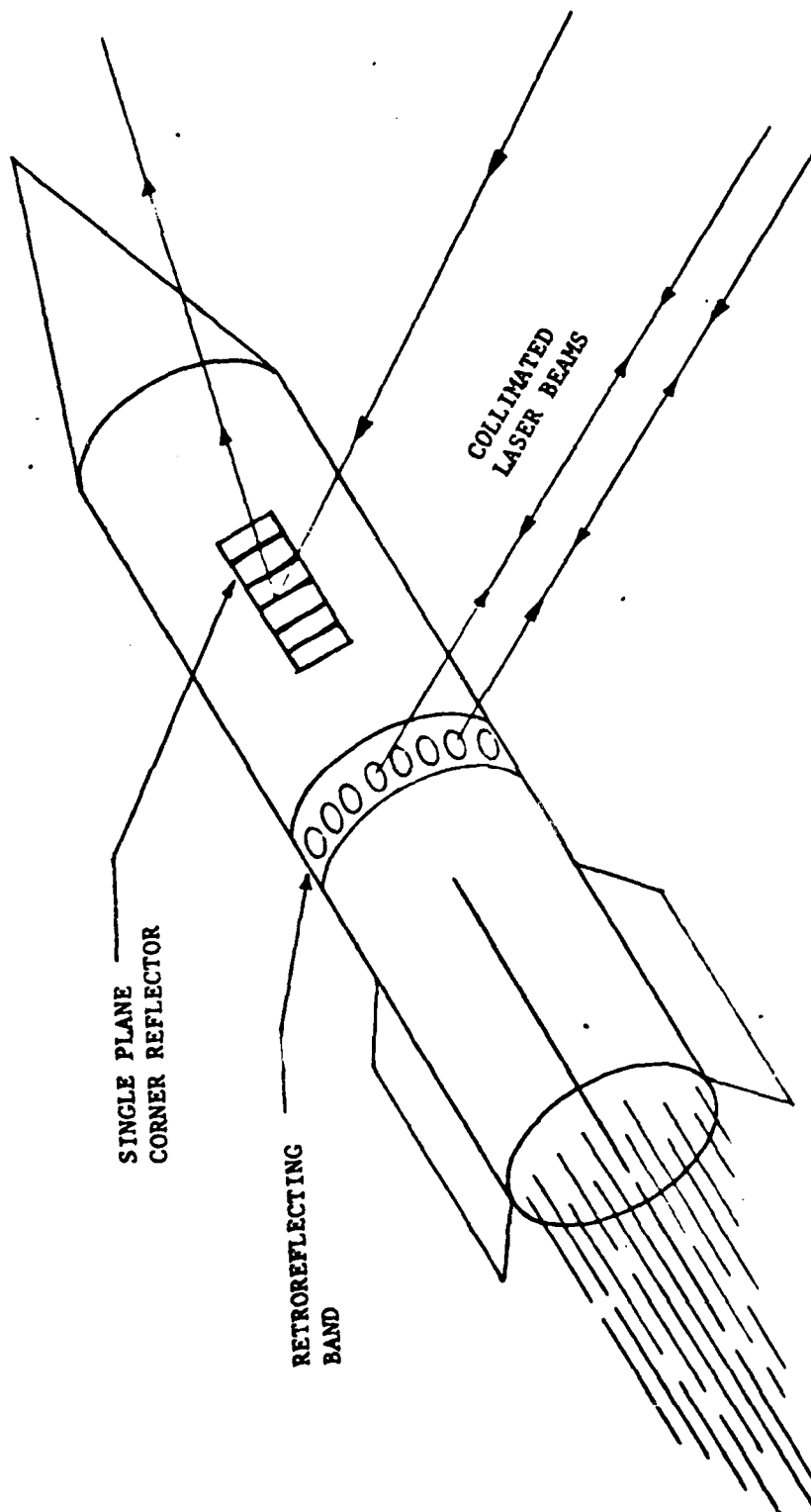


FIGURE 2 - ILLUSTRATION OF VEHICLE SHOWING RETROREFLECTORS

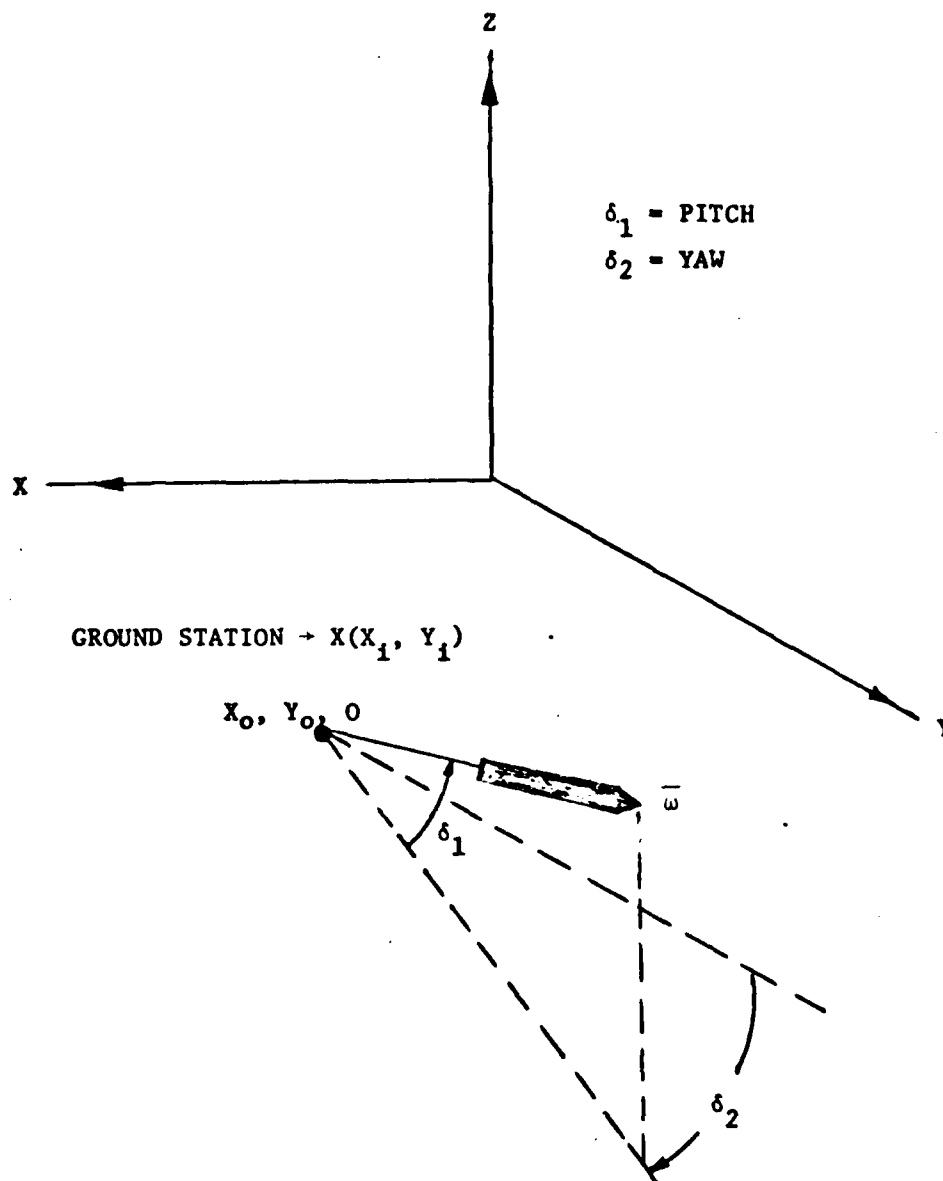


FIGURE 3 - X, Y, Z COORDINATE SYSTEM

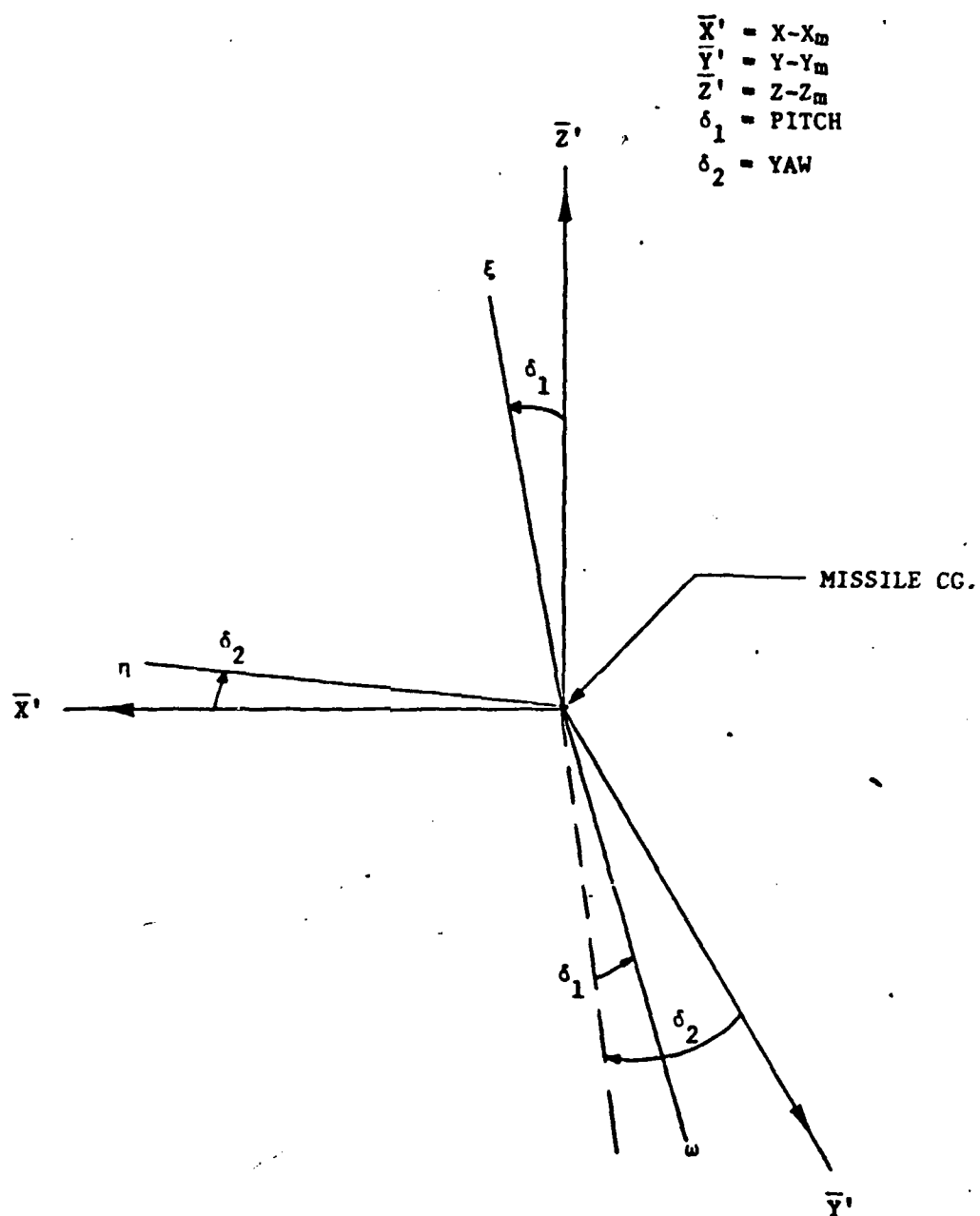


FIGURE 4 -  $\bar{X}'$ ,  $\bar{Y}'$ ,  $\bar{Z}'$  COORDINATE SYSTEM



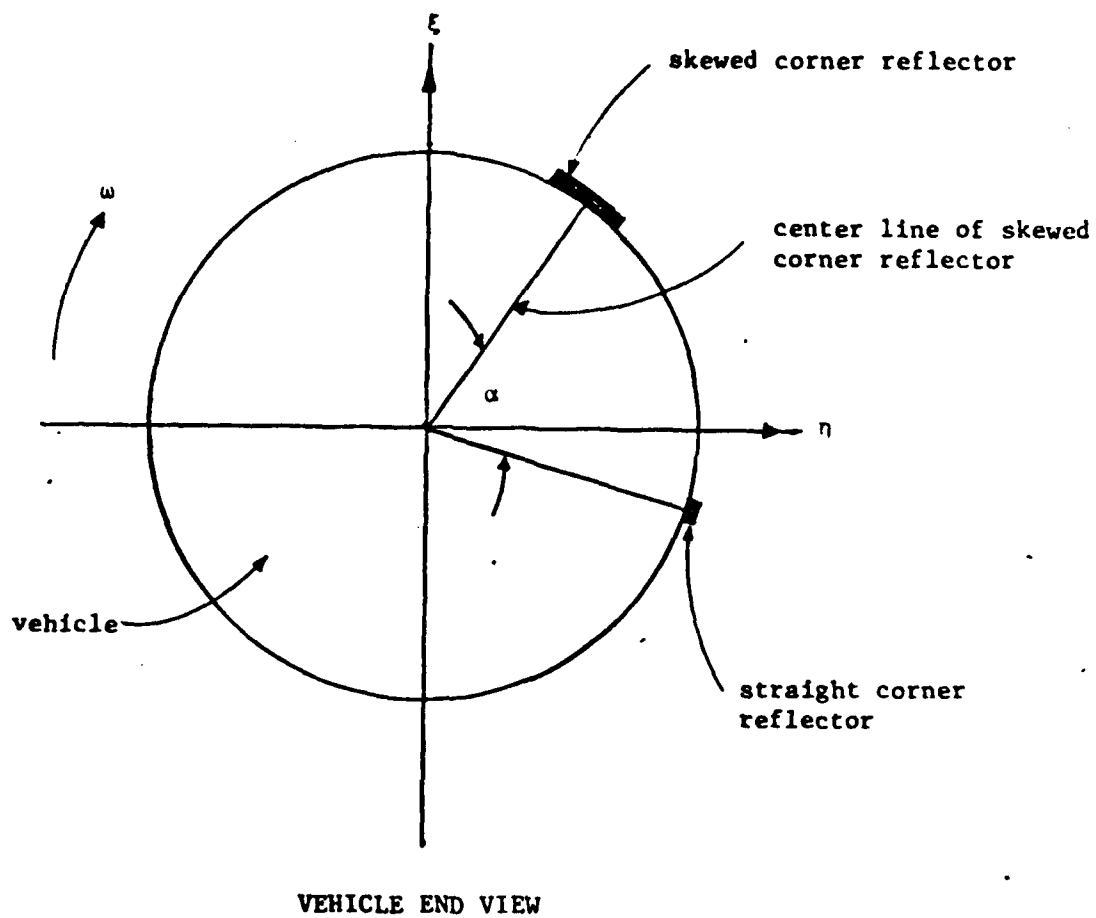
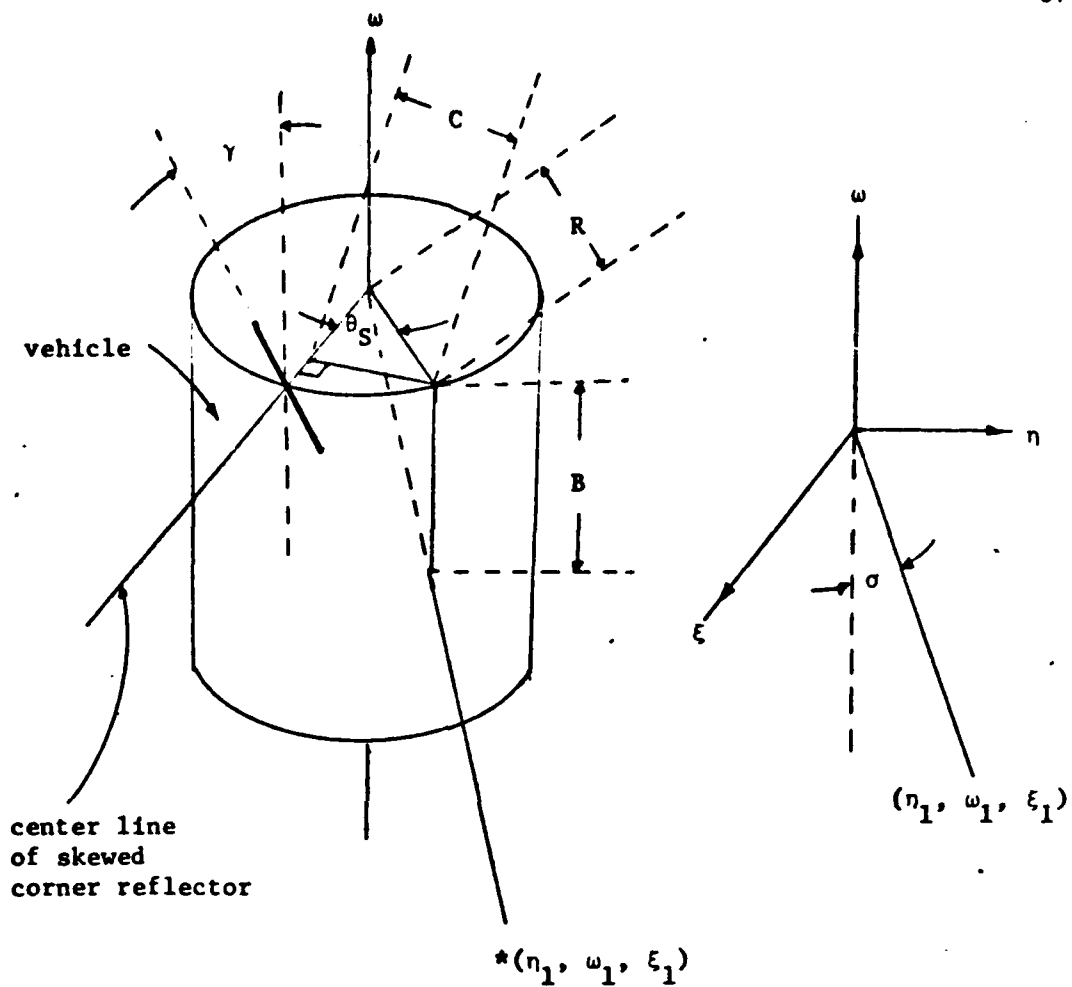


FIGURE 5 - CORNER REFLECTOR GEOMETRY RELATIVE TO VEHICLE



$$\tan(\gamma) = \frac{C}{B}$$

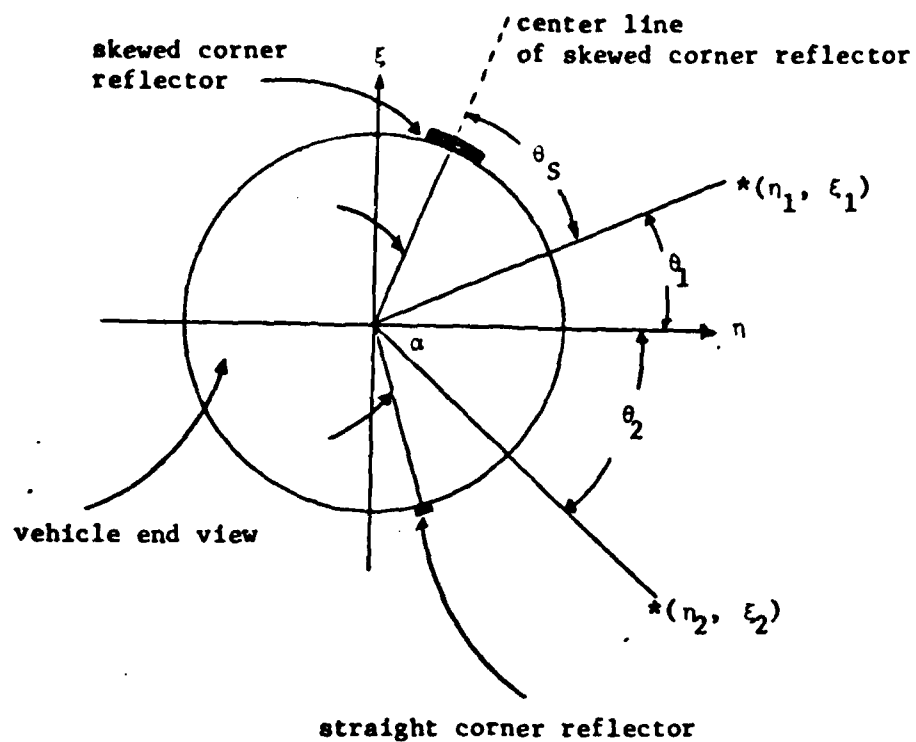
$$\tan(\sigma) = \frac{R}{B}$$

$$\sin(\theta_S) = \frac{C}{R}$$

$$\sin(\theta_S) = \frac{\tan(\gamma)}{\tan(\sigma)}$$

$$\tan(\sigma) = \frac{\omega_1}{(\eta_1^2 + \epsilon_1^2)^{\frac{1}{2}}}$$

FIGURE 6 - GEOMETRY FOR ANALYSIS



$$\Omega \Delta t_{11} = 2\pi - (\alpha - \theta_s)$$

$$\Omega \Delta t_{21} = \theta_1 - \theta_2$$

FIGURE 7 - GEOMETRY FOR ANALYSIS  
FROM VEHICLE END VIEW

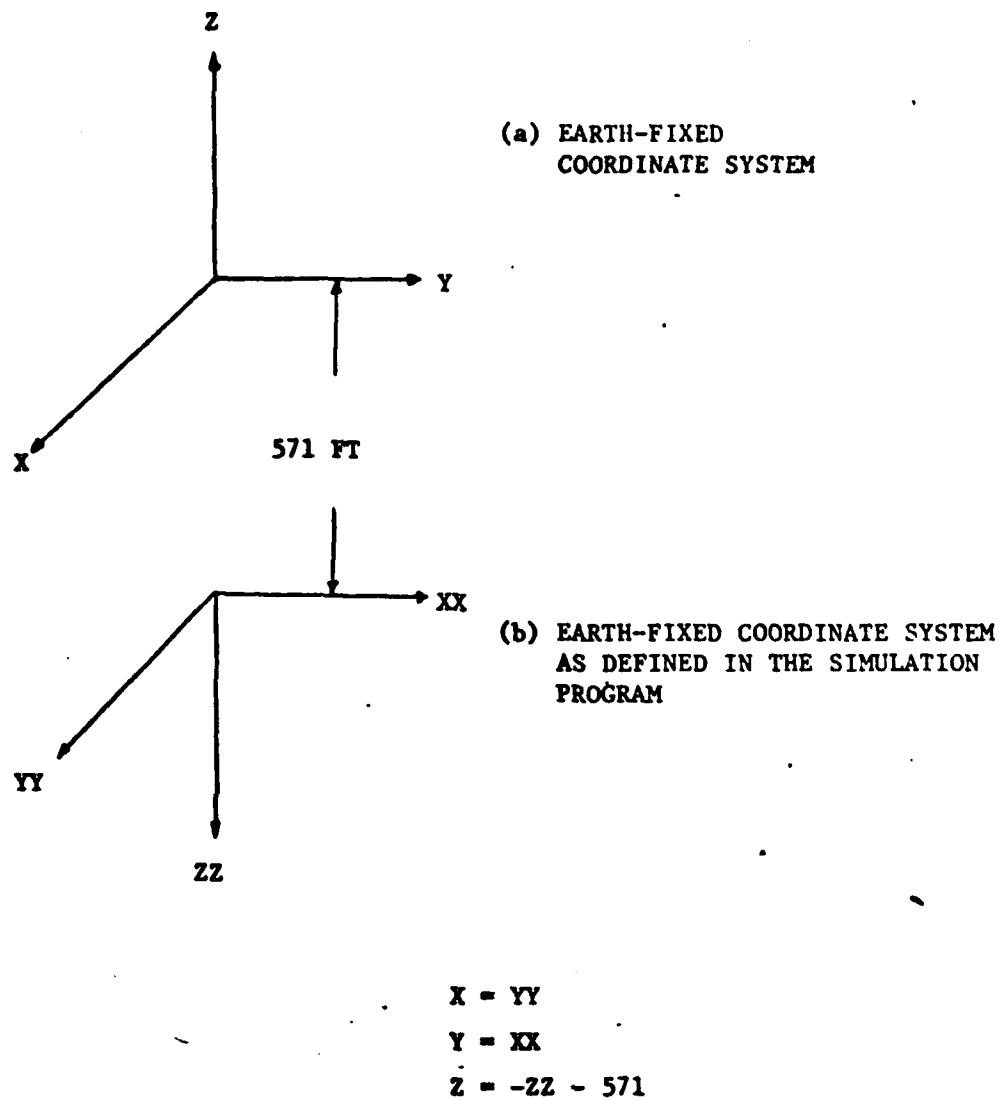


FIGURE 8 - RELATIONSHIPS BETWEEN TWO EARTH-FIXED  
COORDINATE SYSTEMS

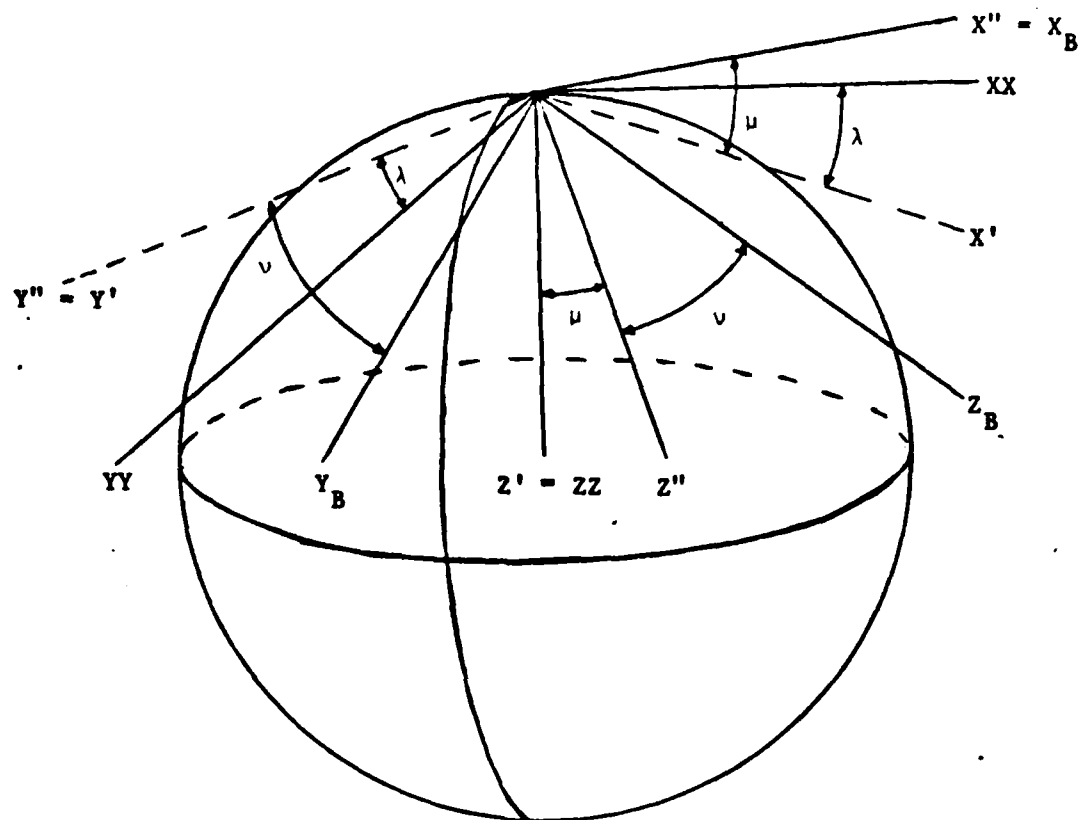


FIGURE 9 - RELATIONSHIP BETWEEN THE BODY FIXED  
AND THE EARTH-FIXED COORDINATE SYSTEM

A rotation about the  $ZZ$ -axis through the angle  $\lambda$  produces the  $X'Y'Z'$  -coordinate system where  $Z' = ZZ$ . Then a rotation about  $Y'$  through the angle  $\mu$  produces the  $X''Y''Z''$  -coordinate system where  $Y'' = Y'$ . Finally, a rotation about the  $X''$  -axis through the angle  $\nu$  produces the  $X'_B Y'_B Z'_B$  -coordinate system.

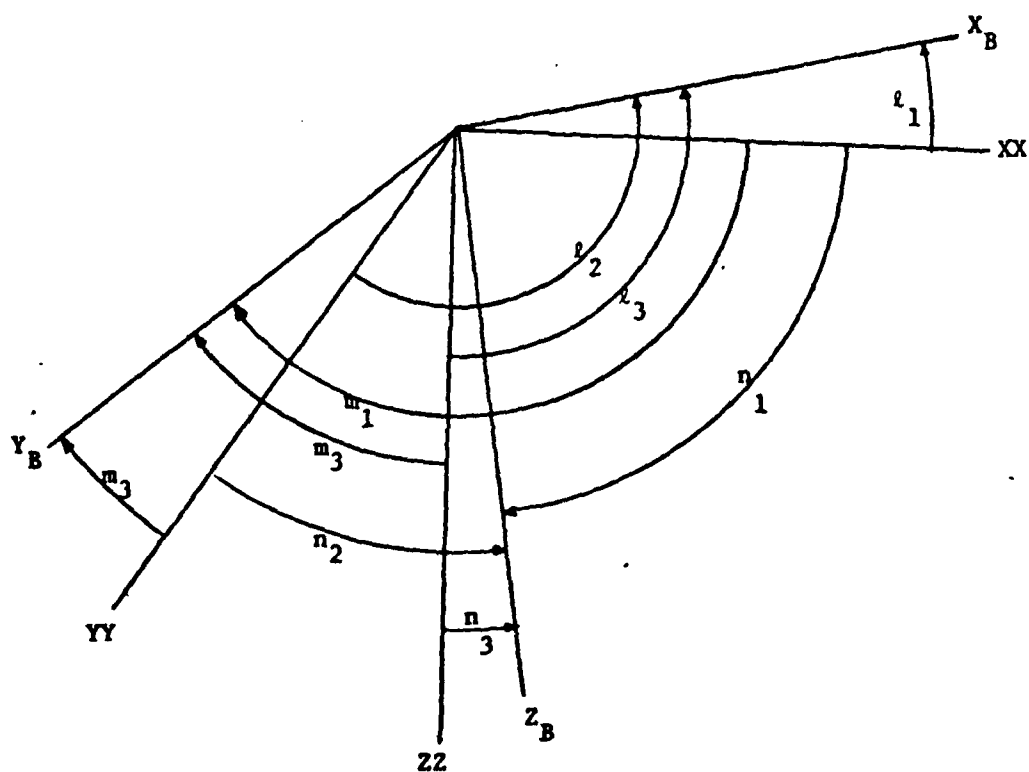


FIGURE 10 - DEFINITION OF DIRECTION COSINES

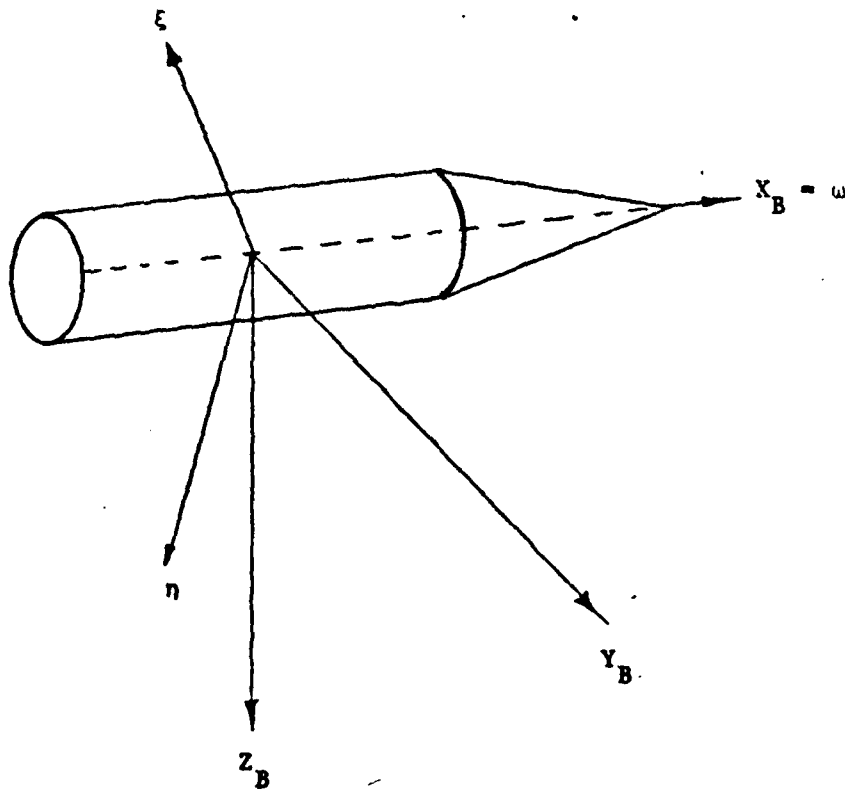
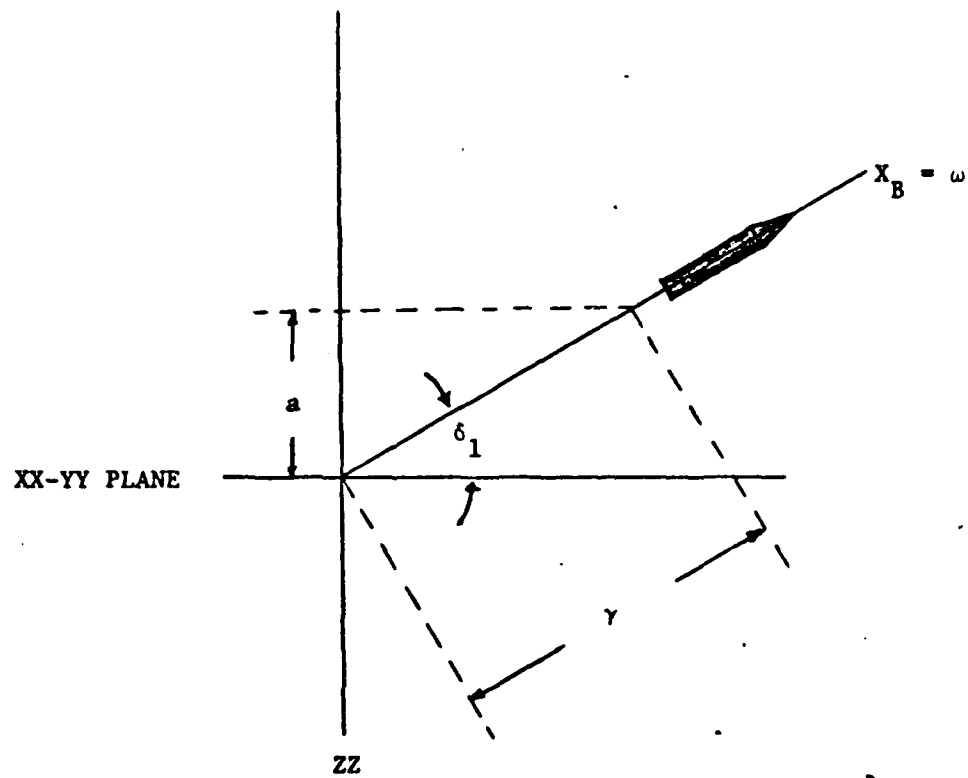


FIGURE 11 - DIFFERENCE BETWEEN  $n\omega\epsilon$  AND THE  
BODY-FIXED COORDINATE SYSTEM

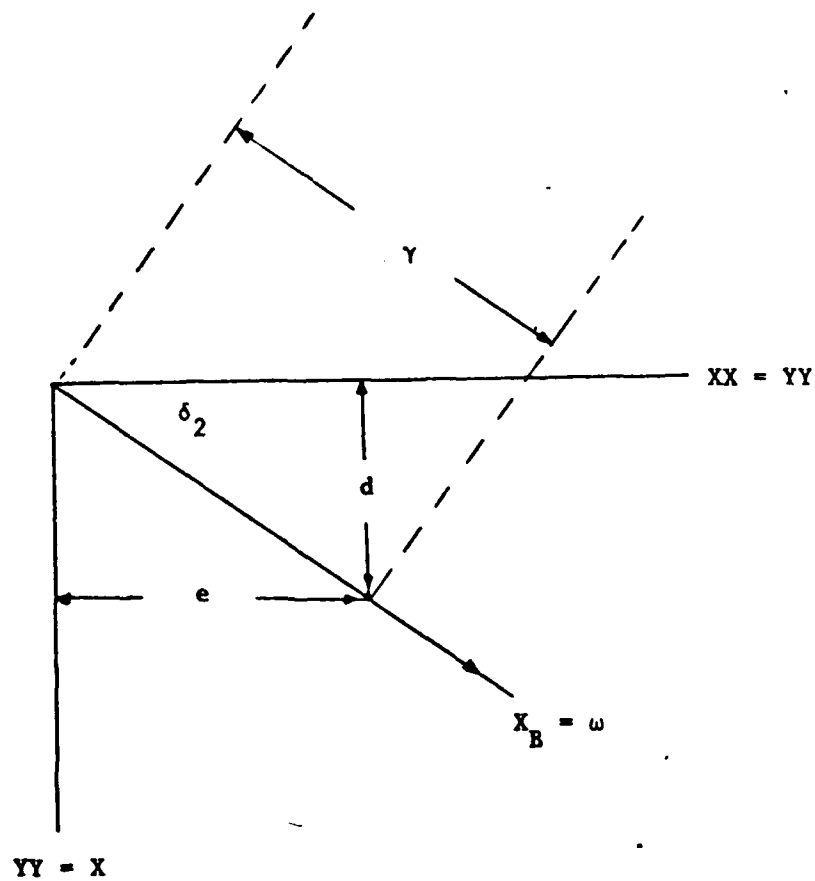
$n$ -axis always parallel to  $X$ - $Y$  plane,  $Y_B$  and  $Z_B$  axis rotate at the same angular velocity as the vehicle does.



$$\sin(\delta_1) = \frac{a}{\gamma} = -l_3$$

FIGURE 12 - PITCH ANGLE IN TERMS OF  
DIRECTION COSINES





$$\tan(\delta_2) = \frac{d}{e} = \frac{d/r}{e/r} = \frac{l_2}{l_1}$$

FIGURE 13 - YAW ANGLE IN TERMS OF DIRECTION COSINES

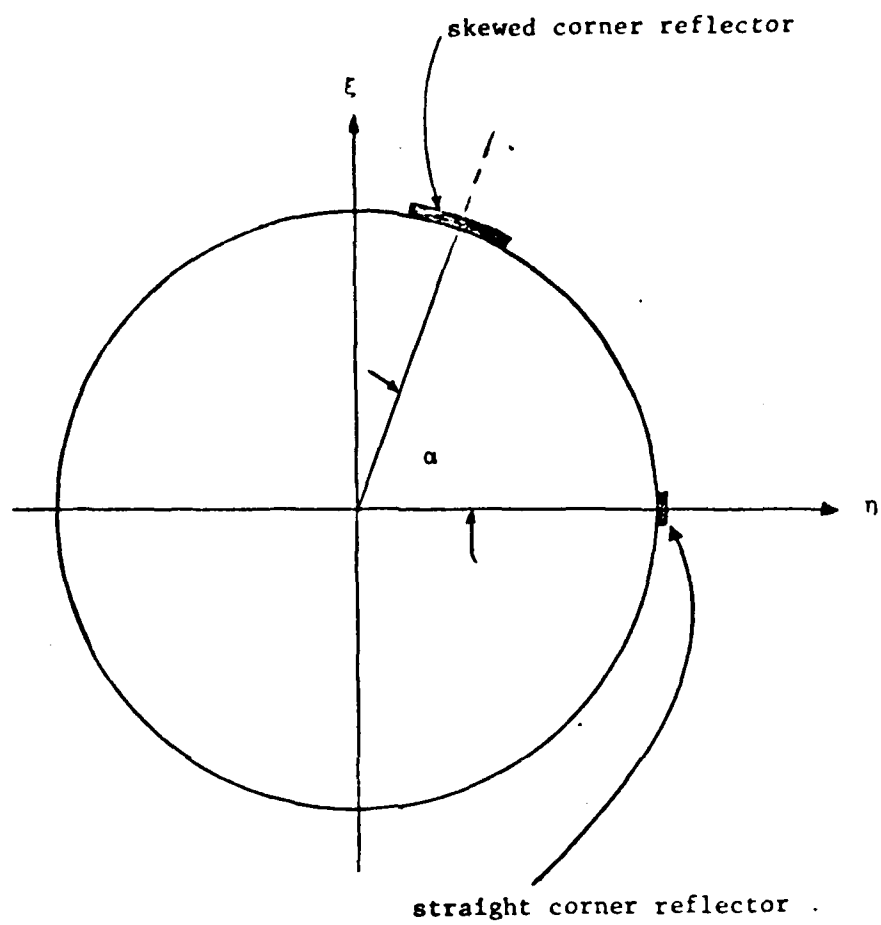
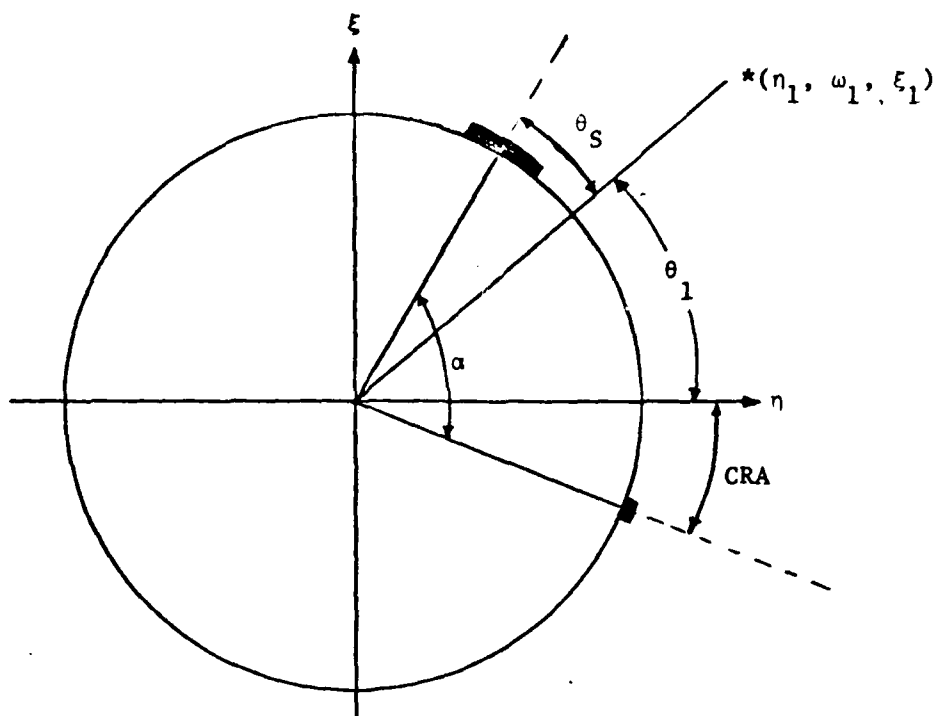
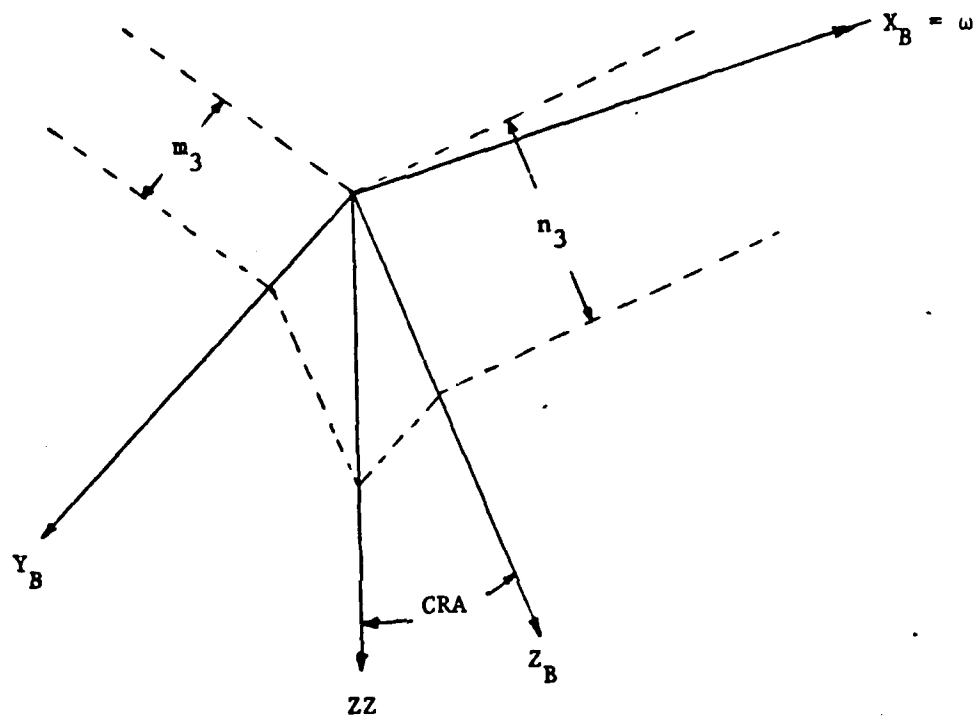


FIGURE 14 - GEOMETRY OF CORNER REFLECTOR AT  $t = 0$



$$\alpha - \theta_S = \theta_1 + \text{CRA}$$

FIGURE 15 - GEOMETRY RELATING TO THE CORNER  
REFLECTOR ANGLE



$$\tan(CRA) = \frac{m_3}{n_3}$$

FIGURE 16 - CORNER REFLECTOR ANGLE IN TERMS  
OF DIRECTION COSINES

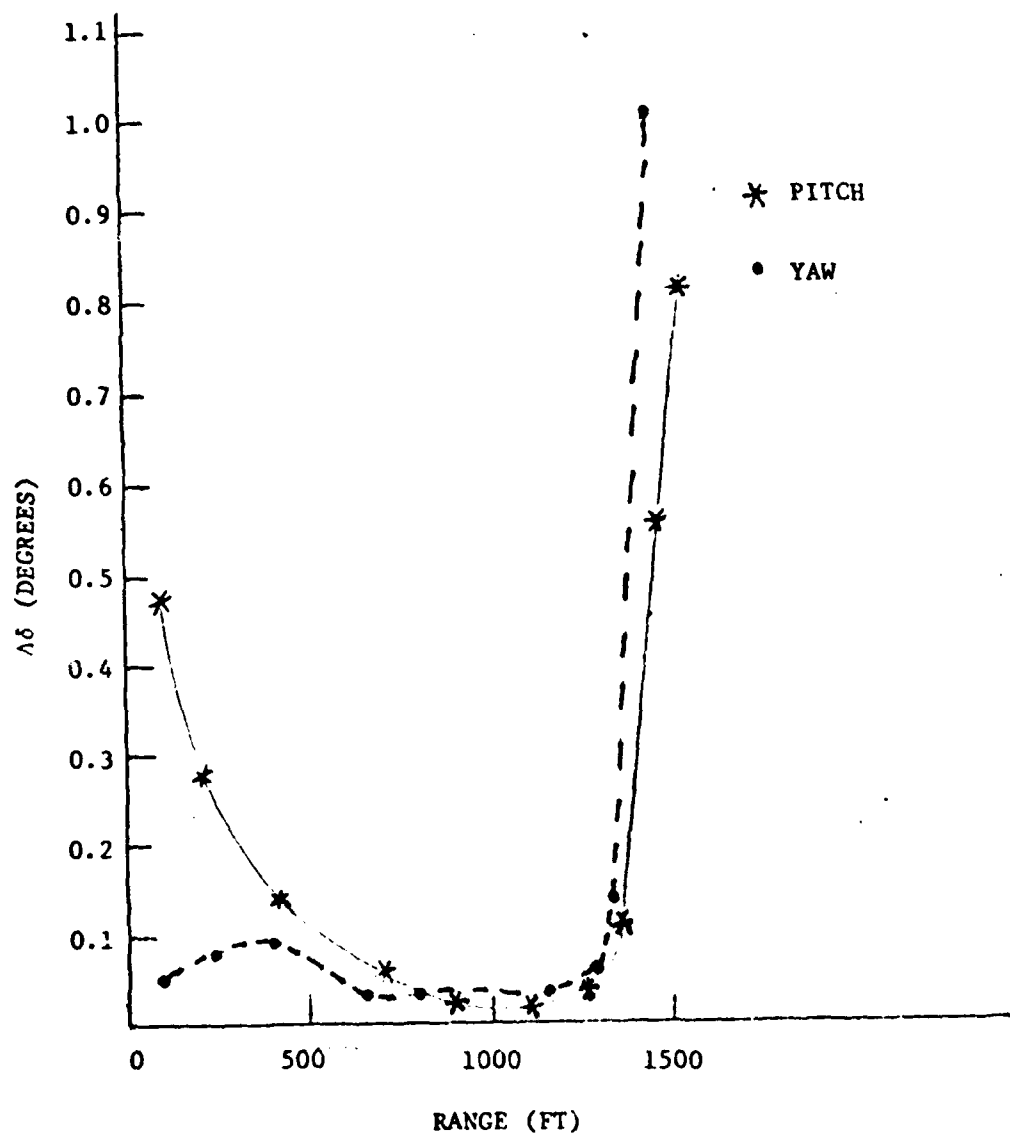


FIGURE 17 - PITCH AND YAW OF ERROR DISTRIBUTION  
WITH DOWNRANGE DISTANCE

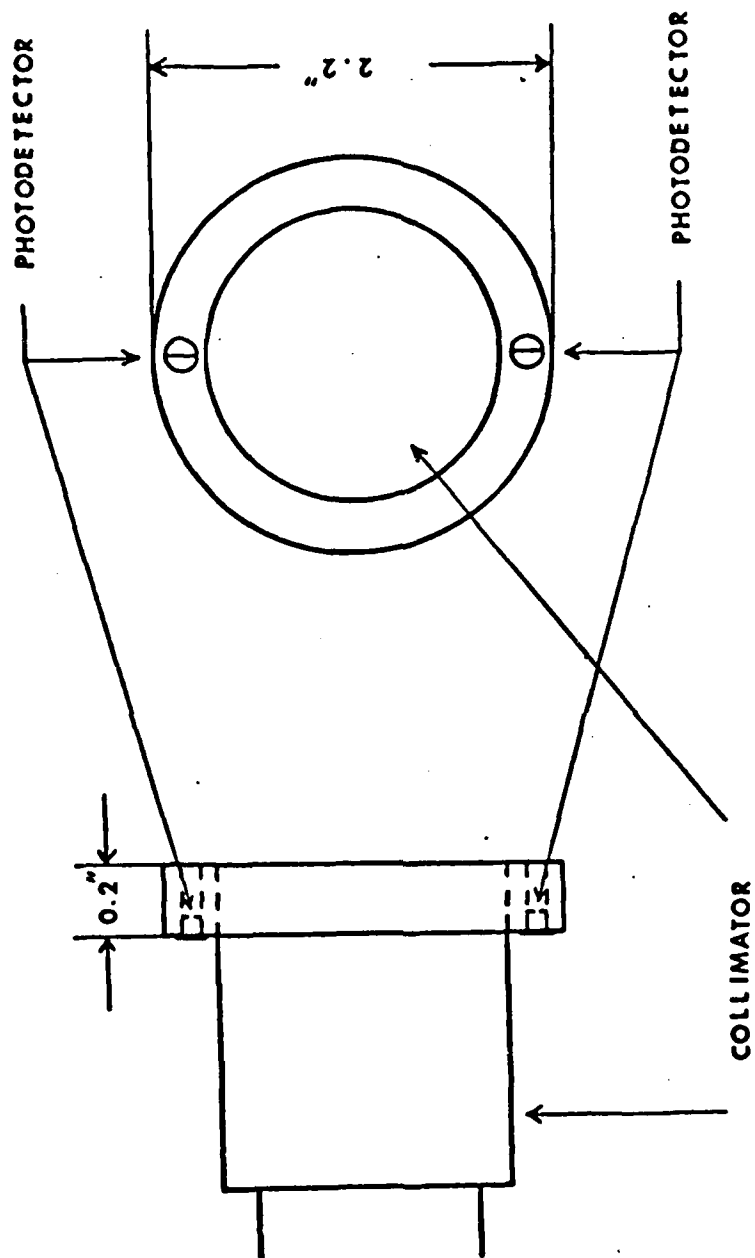


Figure 18. Schematic Drawing of Ring for Detectors

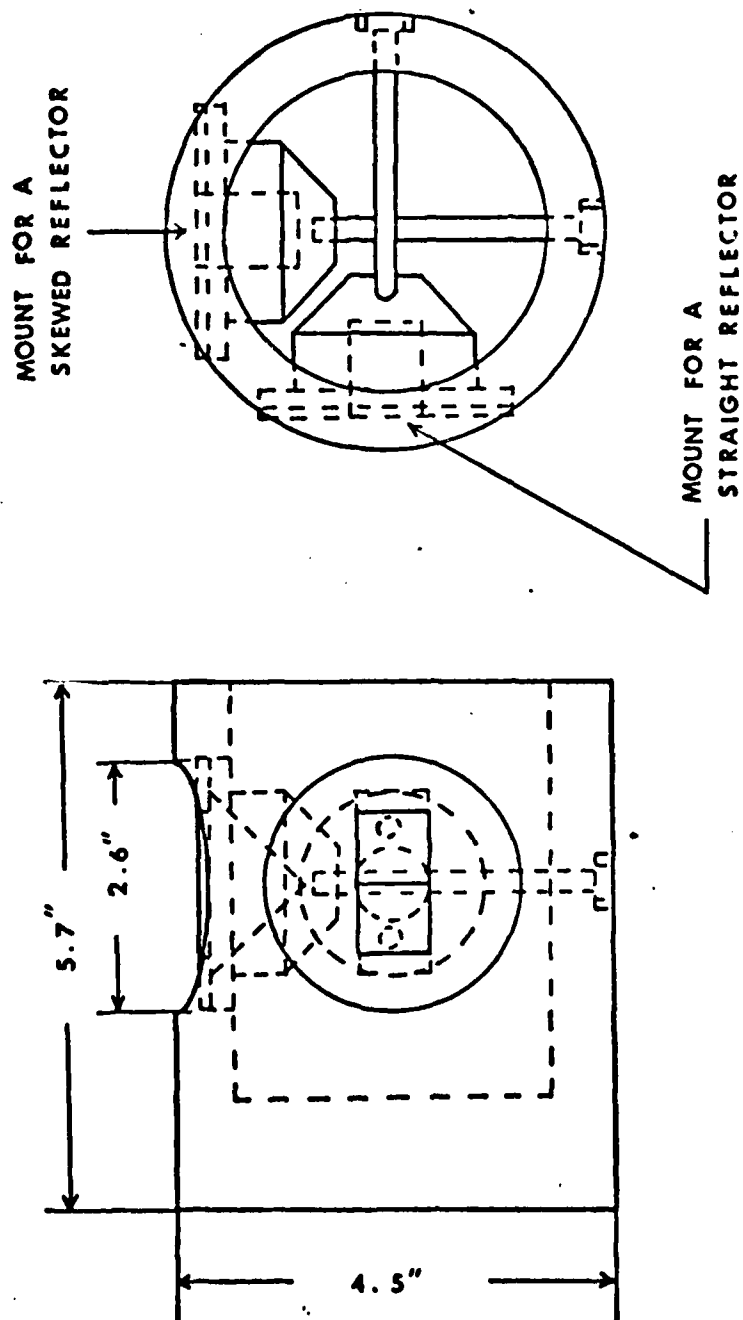


Figure 19. Schematic Drawing of Rocket Body

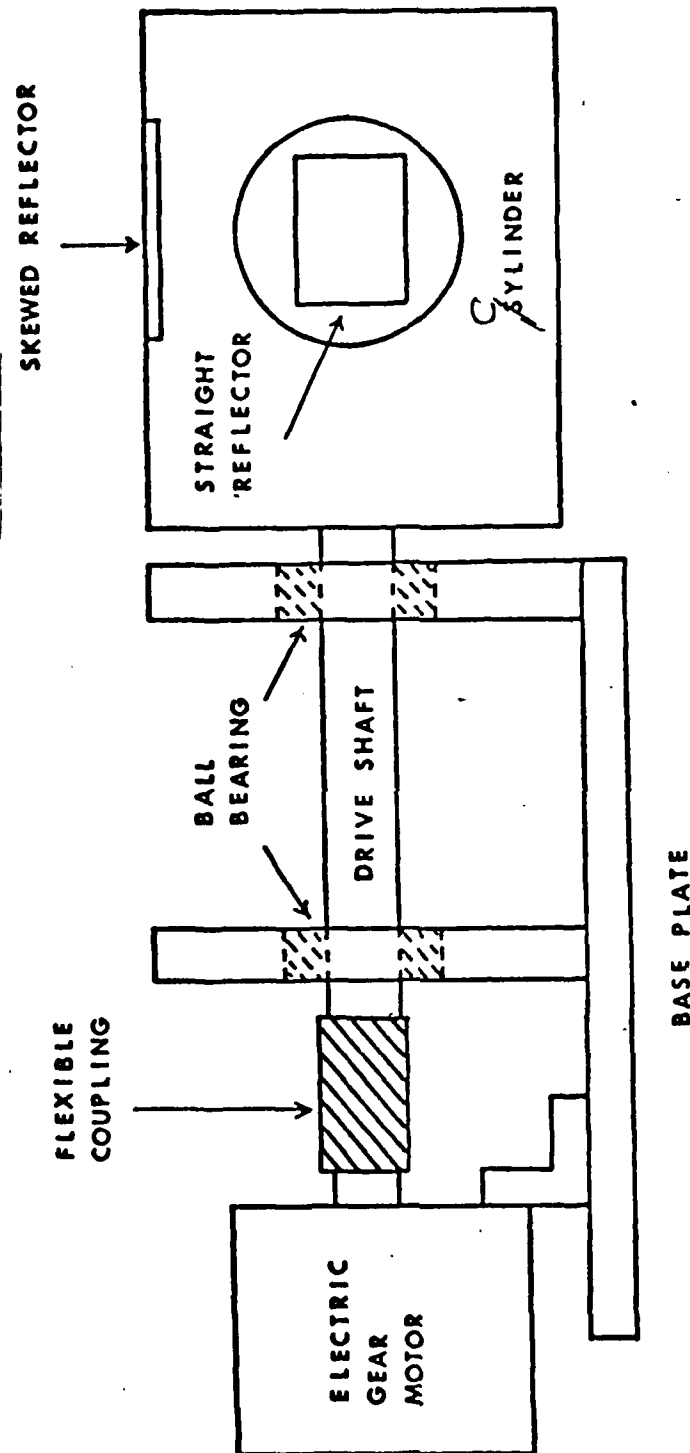


Figure 20. Schematic Drawing of Rocket Model



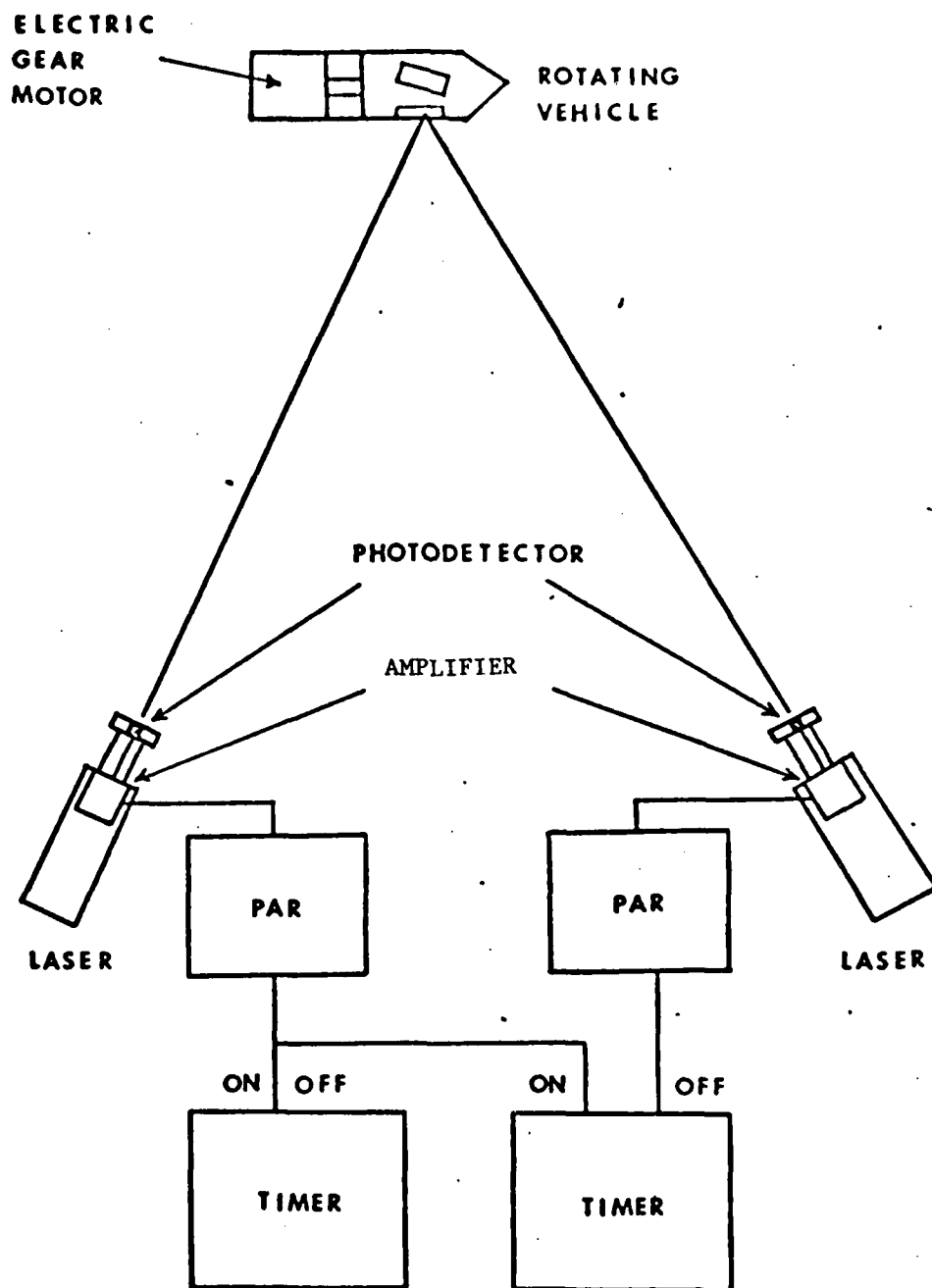


Figure 21. Schematic Representation of Detection/Timing Circuit